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CS/EE 217

GPU Architecture and Parallel Programming

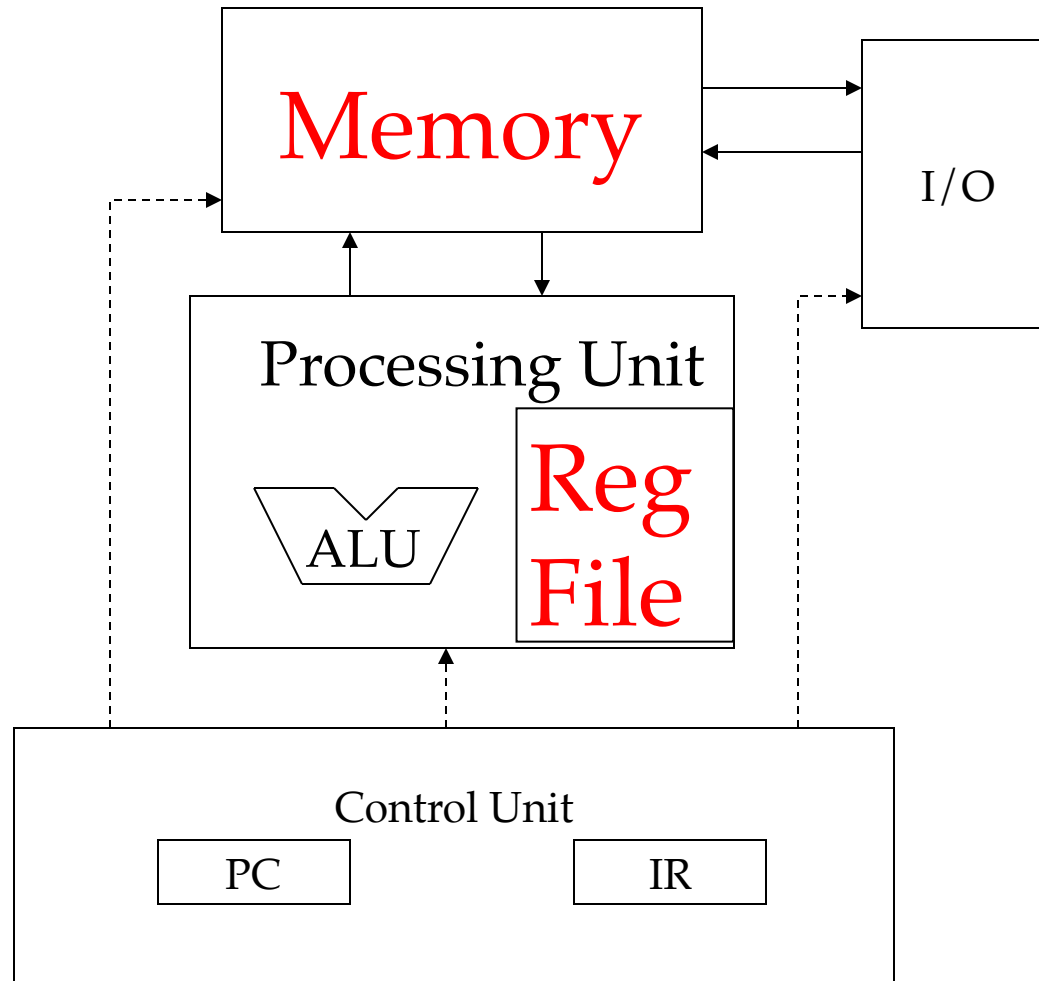
Lectures 4 and 5:

Memory Model and Locality

Objective

- To learn to efficiently use the important levels of the CUDA memory hierarchy
 - Registers, shared memory, global memory
 - Tiled algorithms and barrier synchronization

The Von-Neumann Model



Going back to the program

- Every instruction needs to be fetched from memory, decoded, then executed.
 - The decode stage typically accesses register file
- Instructions come in three flavors: Operate, Data transfer, and Program Control Flow.
- An example instruction cycle is the following:

Fetch | Decode | Execute | Memory

Operate Instructions

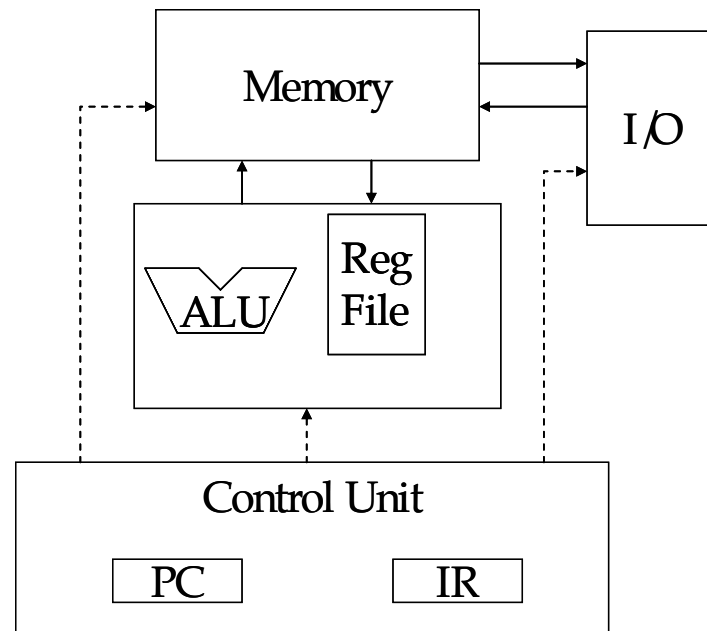
- Example of an operate instruction:
ADD R1, R2, R3
- Instruction cycle for an operate instruction:
Fetch | Decode | Execute | Memory

Memory Access Instructions

- Examples of memory access instruction:
LDR R1, R2, #2
STR R1, R2, #2
- Instruction cycle for an operate instruction:
Fetch | Decode | Execute | Memory

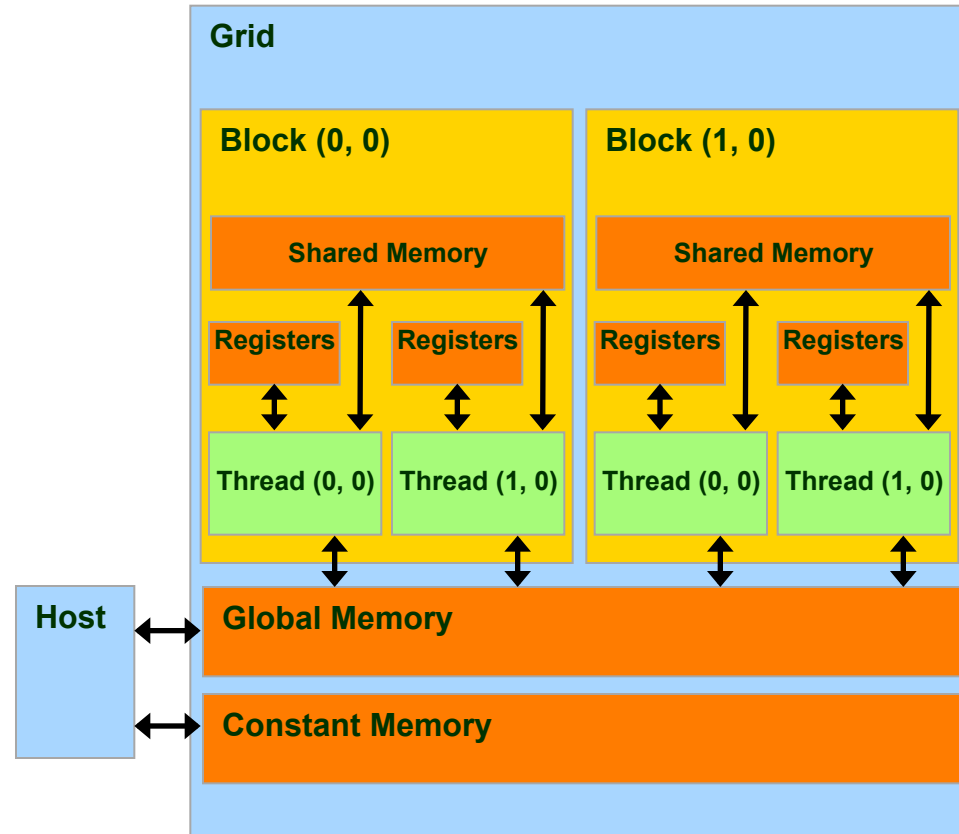
Registers vs Memory

- Registers are “free”
 - No additional memory access instruction
 - Very fast to use, however, there are very few of them
- Memory is expensive (slow), but very large



Programmer View of CUDA Memories

- Each thread can:
 - Read/write per-thread **registers (~1 cycle)**
 - Read/write per-block **shared memory (~5 cycles)**
 - Read/write per-grid **global memory (~500 cycles)**
 - Read/only per-grid **constant memory (~5 cycles with caching)**



Shared Memory in CUDA

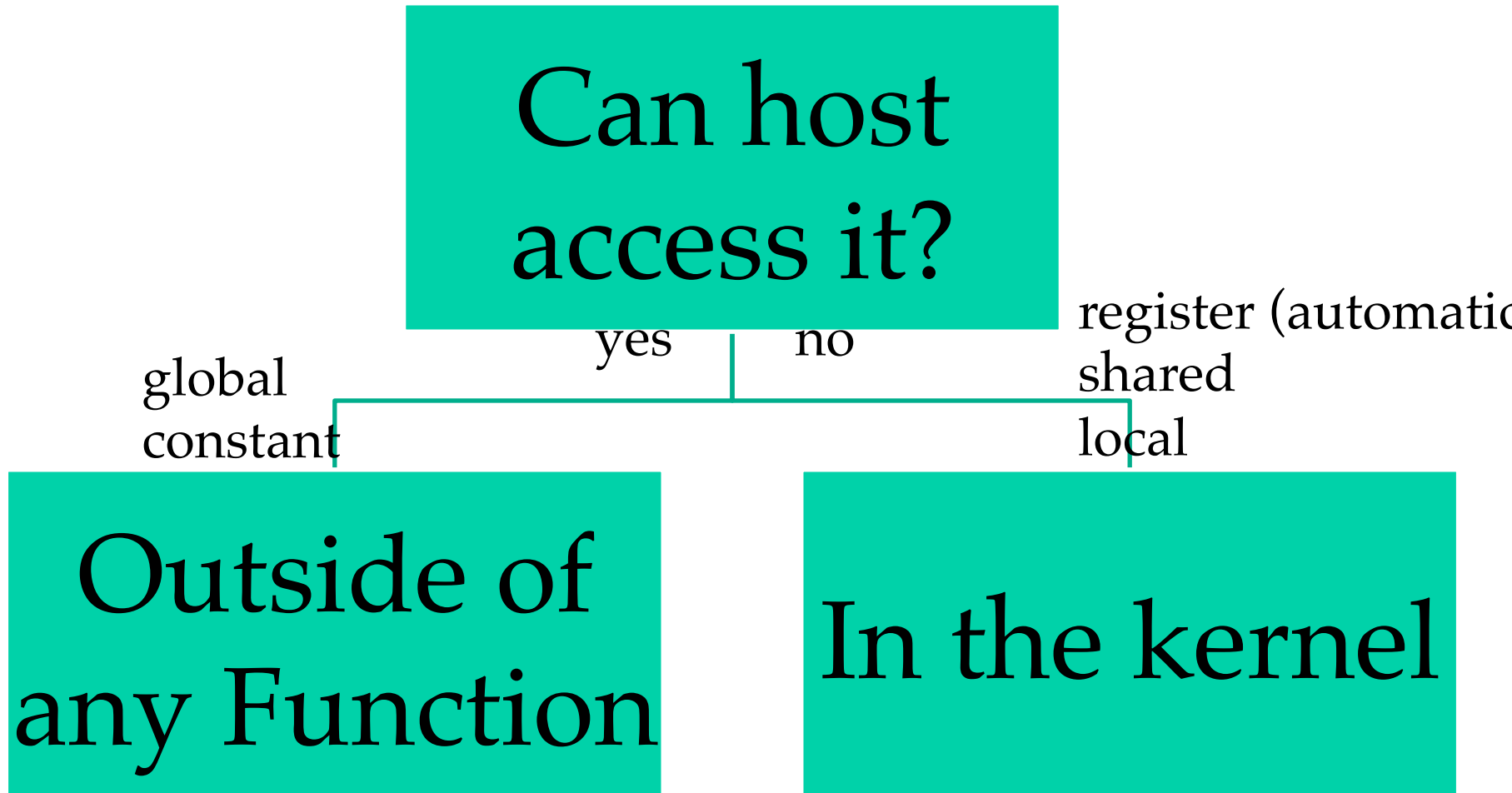
- A special type of memory whose contents are explicitly declared and used in the source code
 - Located in the processor
 - Accessed at much higher speed (in both latency and throughput)
 - Still accessed by memory access instructions
 - Commonly referred to as scratchpad memory in computer architecture

CUDA Variable Type Qualifiers

Variable declaration	Memory	Scope	Lifetime
<code>int LocalVar;</code>	register	thread	thread
<code>__device__ __shared__ int SharedVar;</code>	shared	block	block
<code>__device__ int GlobalVar;</code>	global	grid	application
<code>__device__ __constant__ int ConstantVar;</code>	constant	grid	application

- `__device__` is optional when used with `__shared__`, or `__constant__`
- Automatic variables without any qualifier reside in a register
 - Except per-thread arrays that reside in global memory

Where to Declare Variables?



```
__global__ void MatrixMulKernel(float* d_M, float* d_N, float* d_P, int Width)
{
1.  __shared__ float ds_M[TILE_WIDTH][TILE_WIDTH];
2.  __shared__ float ds_N[TILE_WIDTH][TILE_WIDTH];
```

A Common Programming Strategy

- Global memory resides in device memory (DRAM)
 - slow access
- So, a profitable way of performing computation on the device is to **tile input data** to take advantage of fast shared memory:
 - **Partition** data into **subsets** that fit into shared memory
 - Handle **each data subset with one thread block** by:
 - Loading the subset from global memory to shared memory, **using multiple threads to exploit memory-level parallelism**
 - Performing the computation on the subset from shared memory; each thread can efficiently multi-pass over any data element
 - Copying results from shared memory to global memory

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Matrix-Matrix Multiplication using Shared Memory

Base Matrix Multiplication Kernel

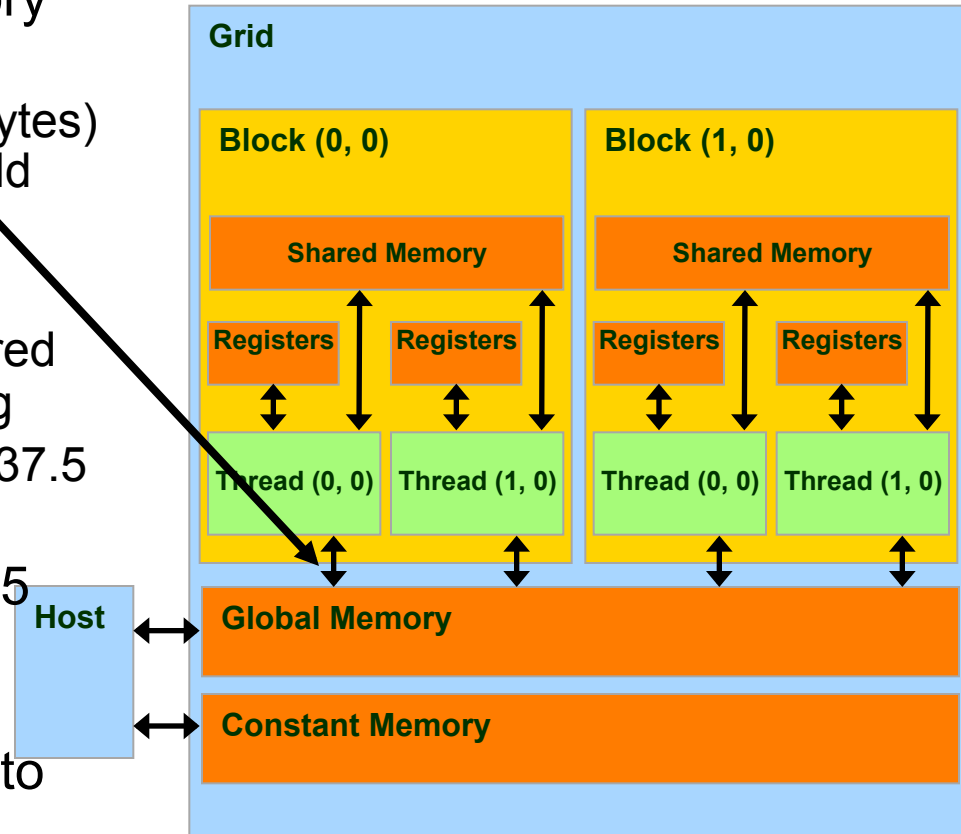
```
__global__ void MatrixMulKernel(float* d_M, float* d_N, float* d_P, int Width)
{
    // Calculate the row index of the Pd element and M
    int Row = blockIdx.y*TILE_WIDTH + threadIdx.y;
    // Calculate the column index of Pd and N
    int Col = blockIdx.x*TILE_WIDTH + threadIdx.x;

    float Pvalue = 0;
    // each thread computes one element of the block sub-matrix
    for (int k = 0; k < Width; ++k)
        Pvalue += d_M[Row*Width+k] * d_N[k*Width+Col];

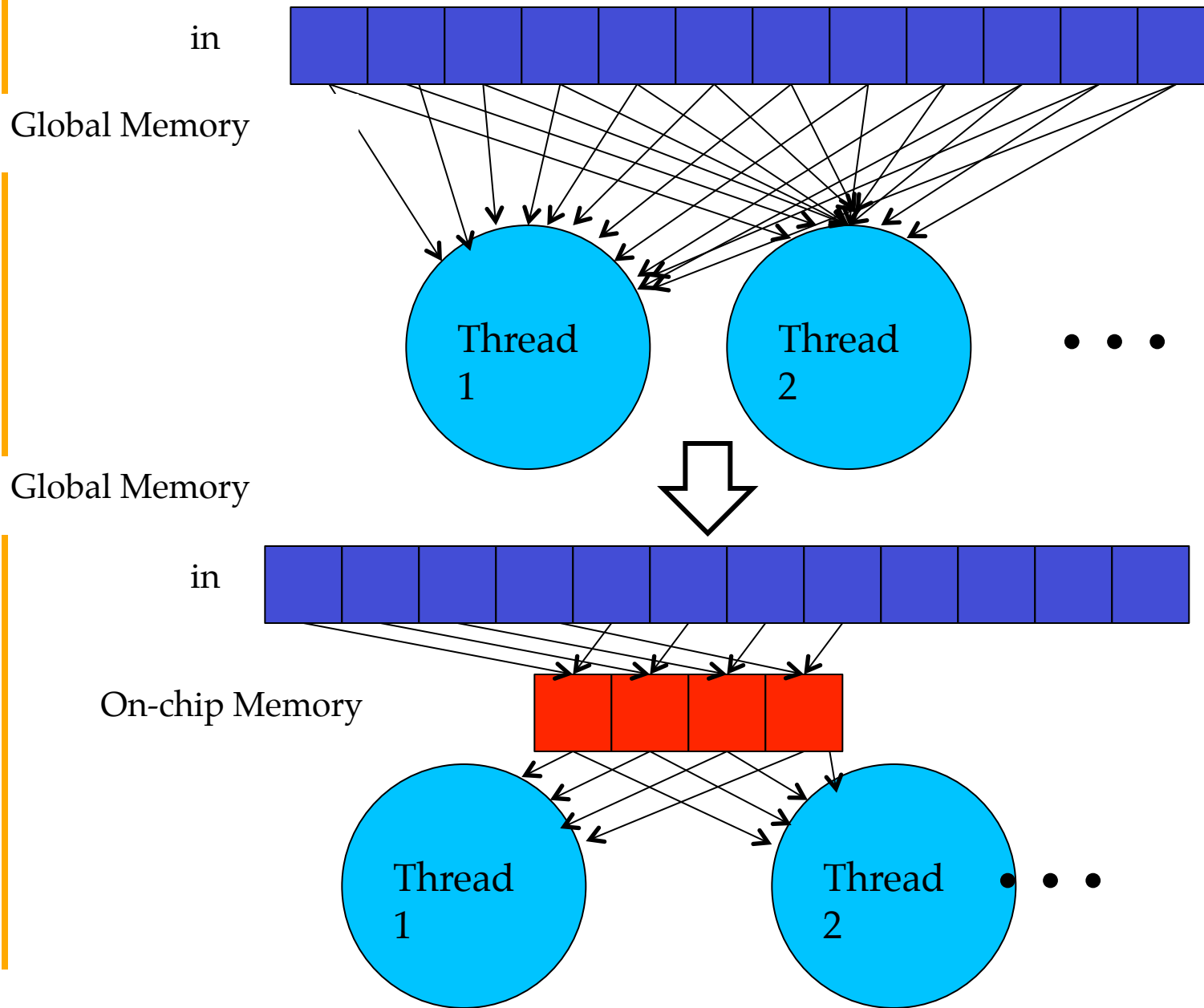
    d_P[Row*Width+Col] = Pvalue;
}
```

How about performance on Fermi?

- All threads access global memory for their input matrix elements
 - Two memory accesses (8 bytes) per floating point multiply-add
 - 4B/s of memory bandwidth/FLOPS
 - $4 \times 1,000 = 4,000$ GB/s required to achieve peak FLOP rating
 - 150 GB/s limits the code at 37.5 GFLOPS
- The actual code runs at about 25 GFLOPS
- Need to drastically cut down memory accesses to get closer to the peak 1,000 GFLOPS



Shared Memory Blocking Basic Idea



Basic Concept of Blocking/Tiling

- In a congested traffic system, significant reduction of vehicles can greatly improve the delay seen by all vehicles
 - Carpooling for commuters
 - Blocking/Tiling for global memory accesses
 - drivers = threads,
 - cars = data



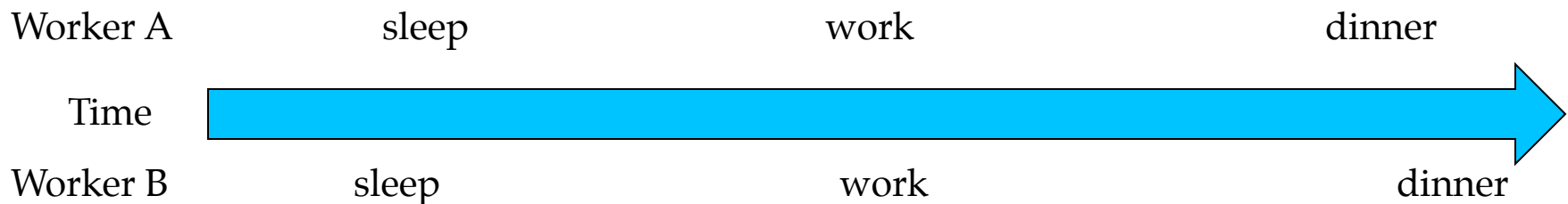
Some computations are more challenging to block/tile than others.

- Some carpools may be easier than others
 - More efficient if neighbors are also classmates or co-workers
 - Some vehicles may be more suitable for carpooling
- Similar variations exist in blocking/tiling

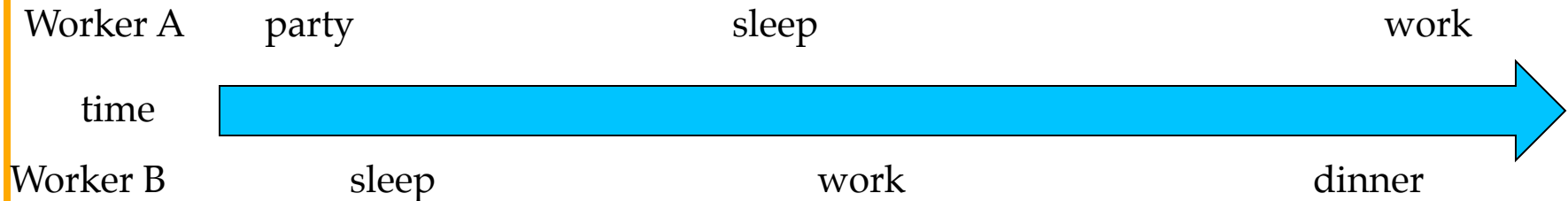


Carpools need synchronization.

- Good – when people have similar schedule

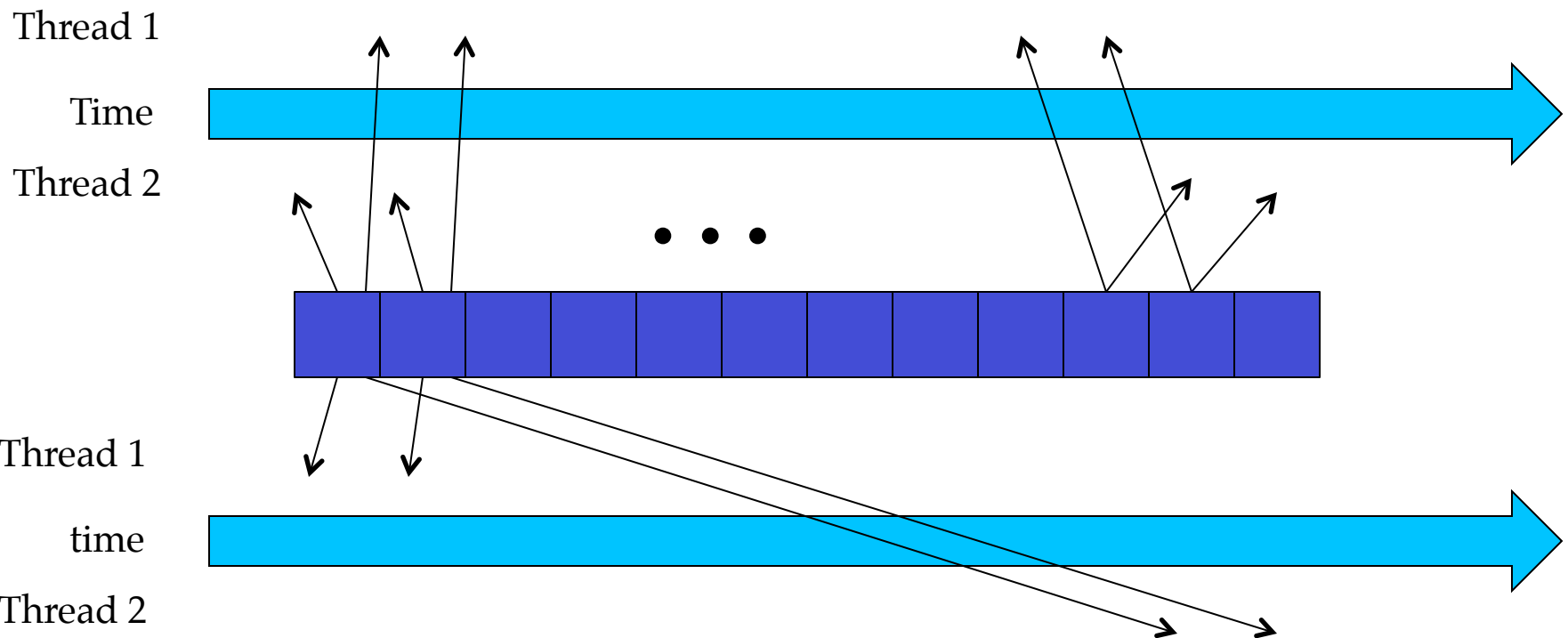


- Bad – when people have very different schedule



Same with Blocking/Tiling

- Good – when threads have similar access timing



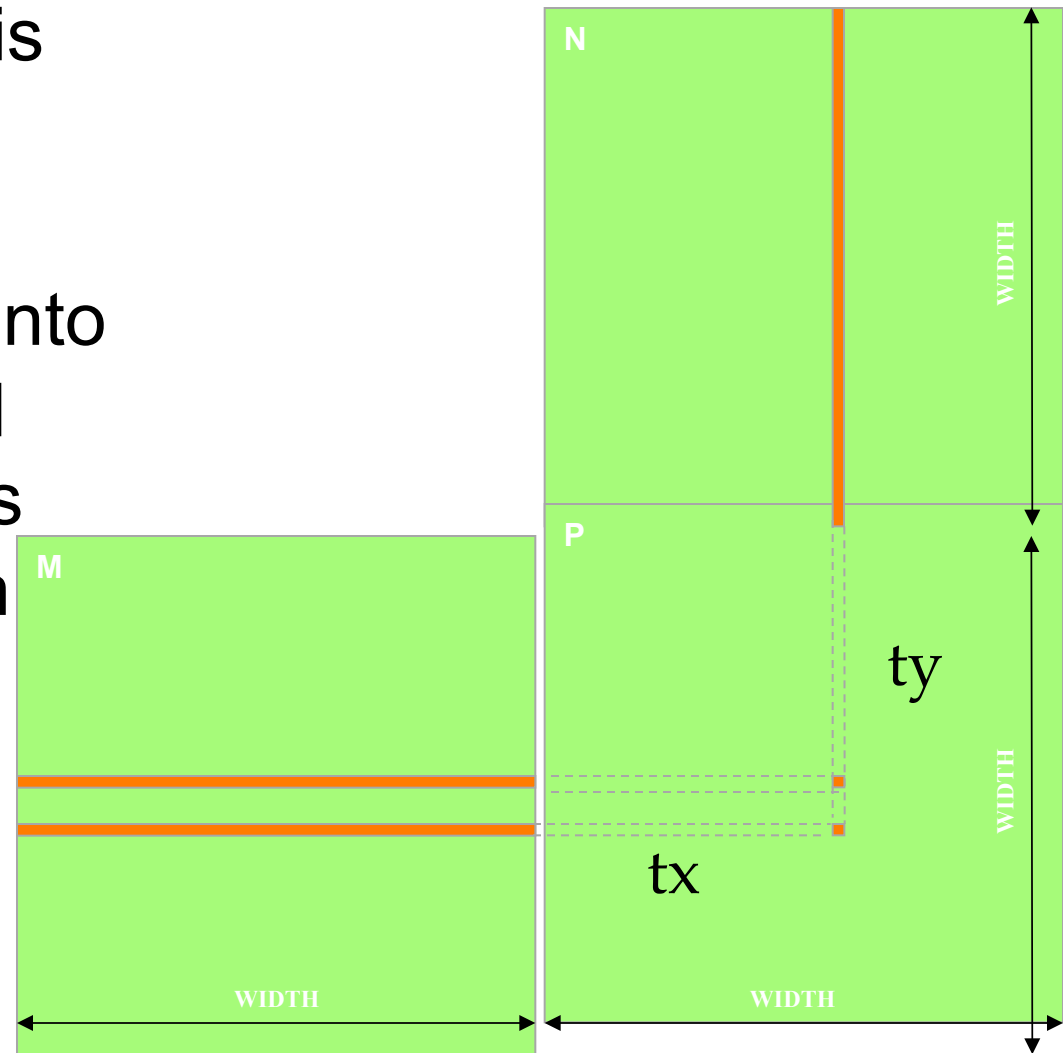
- Bad – when threads have very different timing

Outline of Technique

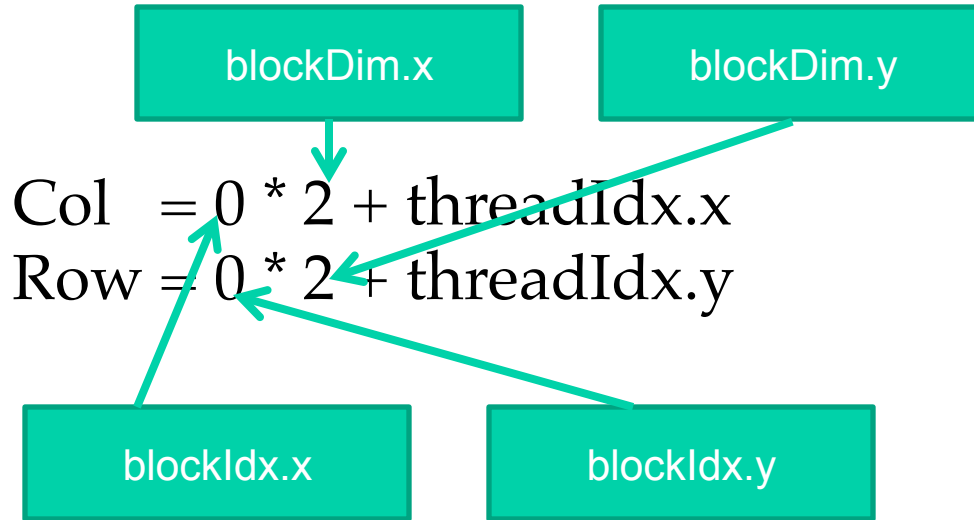
- Identify a block/tile of global memory content that are accessed by multiple threads
- Load the block/tile from global memory into on-chip memory
- Have the multiple threads to access their data from the on-chip memory
- Move on to the next block/tile

Idea: Use Shared Memory to reuse global memory data

- Each input element is read by **WIDTH** threads.
- Load each element into Shared Memory and have several threads use the local version to reduce the memory bandwidth
 - Tiled algorithms



Work for Block (0,0) in a TILE_WIDTH = 2 Configuration



Col = 0
Col = 1

$N_{0,0}$	$N_{0,1}$	$N_{0,2}$	$N_{0,3}$
$N_{1,0}$	$N_{1,1}$	$N_{1,2}$	$N_{1,3}$
$N_{2,0}$	$N_{2,1}$	$N_{2,2}$	$N_{2,3}$
$N_{3,0}$	$N_{3,1}$	$N_{3,2}$	$N_{3,3}$

Row = 0

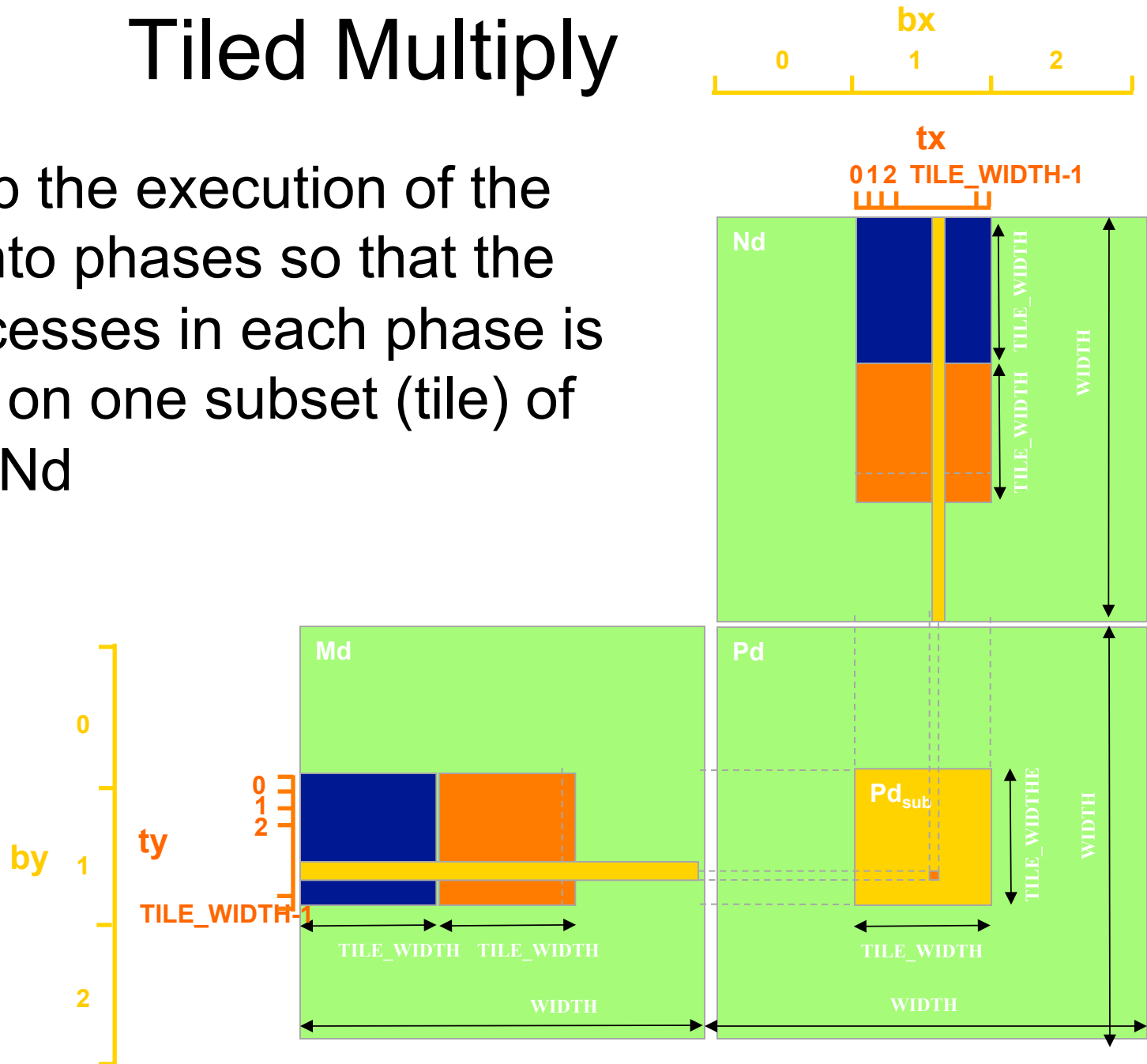
Row = 1

$M_{0,0}$	$M_{0,1}$	$M_{0,2}$	$M_{0,3}$
$M_{1,0}$	$M_{1,1}$	$M_{1,2}$	$M_{1,3}$
$M_{2,0}$	$M_{2,1}$	$M_{2,2}$	$M_{2,3}$
$M_{3,0}$	$M_{3,1}$	$M_{3,2}$	$M_{3,3}$

$P_{0,0}$	$P_{0,1}$	$P_{0,2}$	$P_{0,3}$
$P_{1,0}$	$P_{1,1}$	$P_{1,2}$	$P_{1,3}$
$P_{2,0}$	$P_{2,1}$	$P_{2,2}$	$P_{2,3}$
$P_{3,0}$	$P_{3,1}$	$P_{3,2}$	$P_{3,3}$

Tiled Multiply

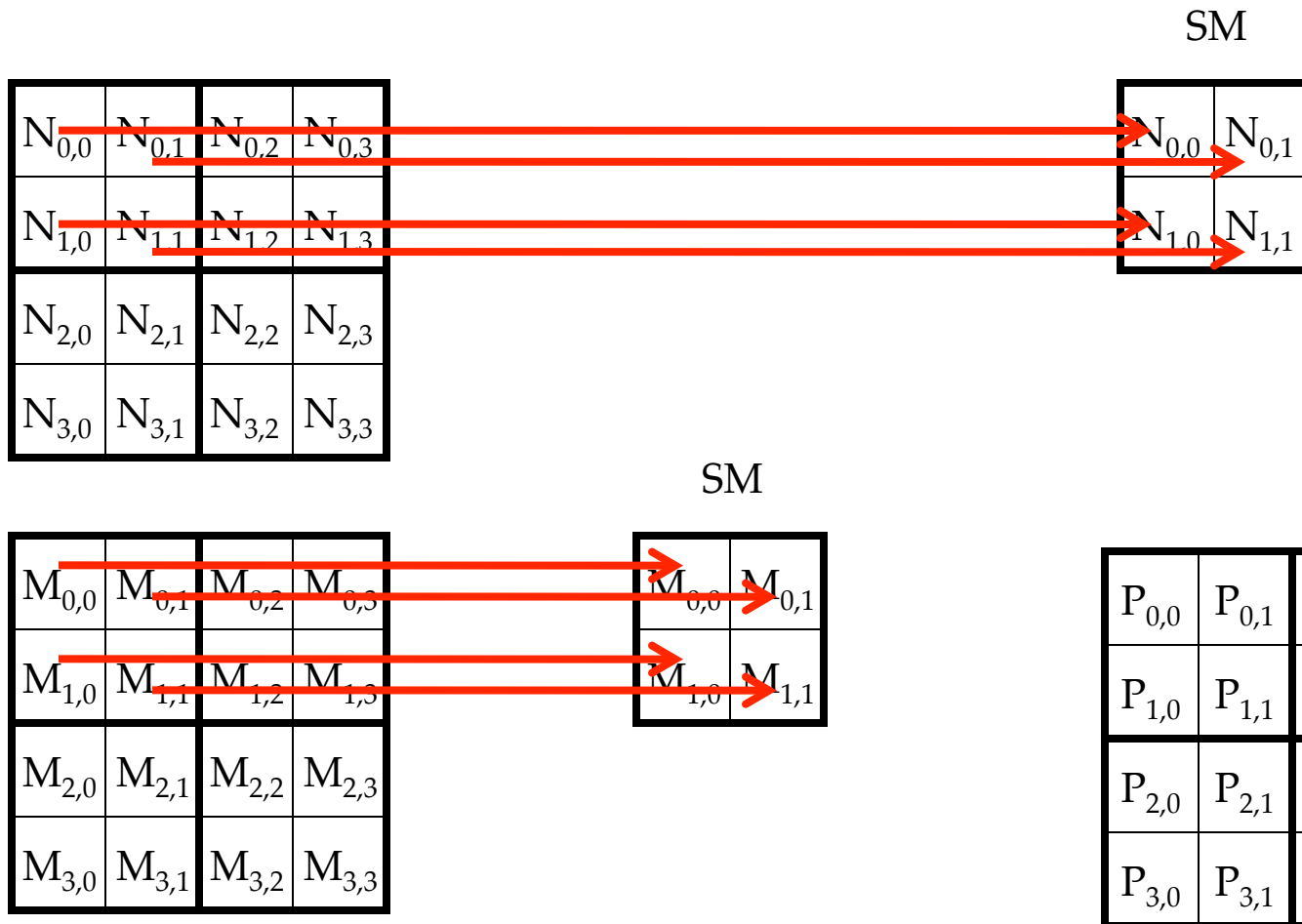
- Break up the execution of the kernel into phases so that the data accesses in each phase is focused on one subset (tile) of M_d and N_d



Loading a Tile

- All threads in a block participate
 - Each thread loads one Md element and one Nd element in based tiled code
- Assign the loaded element to each thread such that the accesses within each warp is coalesced (more later).

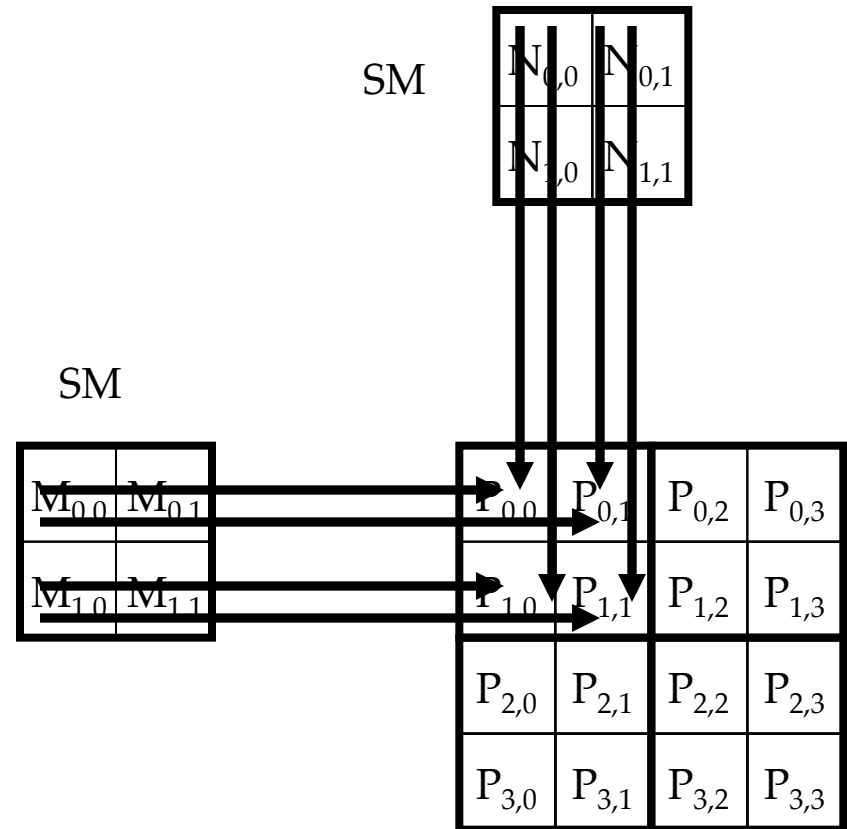
Work for Block (0,0)



Work for Block (0,0)

$N_{0,0}$	$N_{0,1}$	$N_{0,2}$	$N_{0,3}$
$N_{1,0}$	$N_{1,1}$	$N_{1,2}$	$N_{1,3}$
$N_{2,0}$	$N_{2,1}$	$N_{2,2}$	$N_{2,3}$
$N_{3,0}$	$N_{3,1}$	$N_{3,2}$	$N_{3,3}$

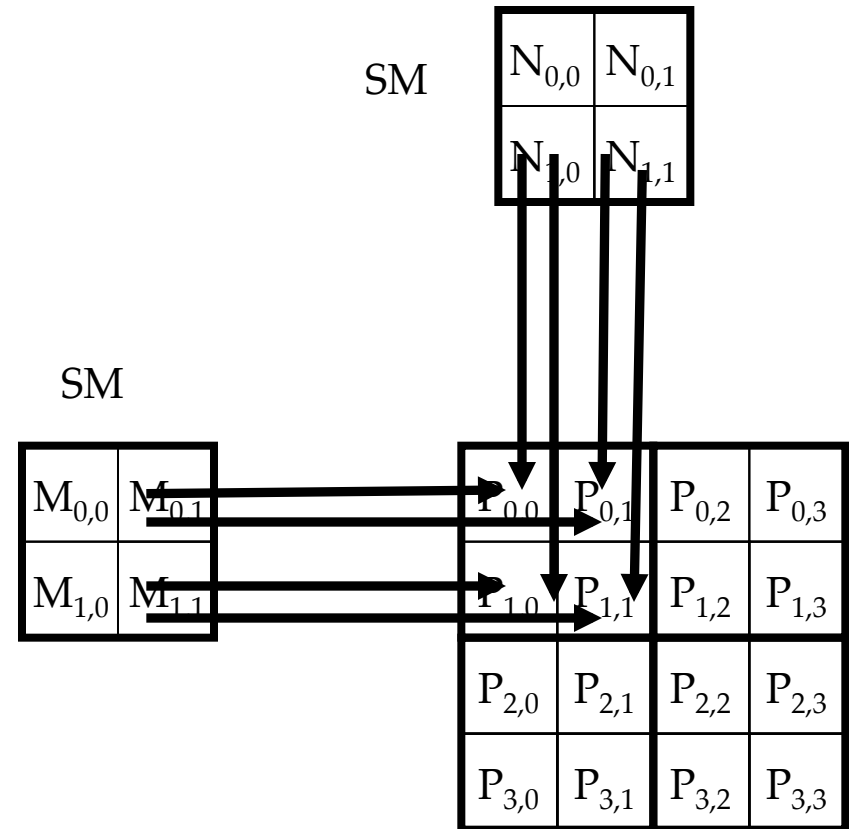
$M_{0,0}$	$M_{0,1}$	$M_{0,2}$	$M_{0,3}$
$M_{1,0}$	$M_{1,1}$	$M_{1,2}$	$M_{1,3}$
$M_{2,0}$	$M_{2,1}$	$M_{2,2}$	$M_{2,3}$
$M_{3,0}$	$M_{3,1}$	$M_{3,2}$	$M_{3,3}$



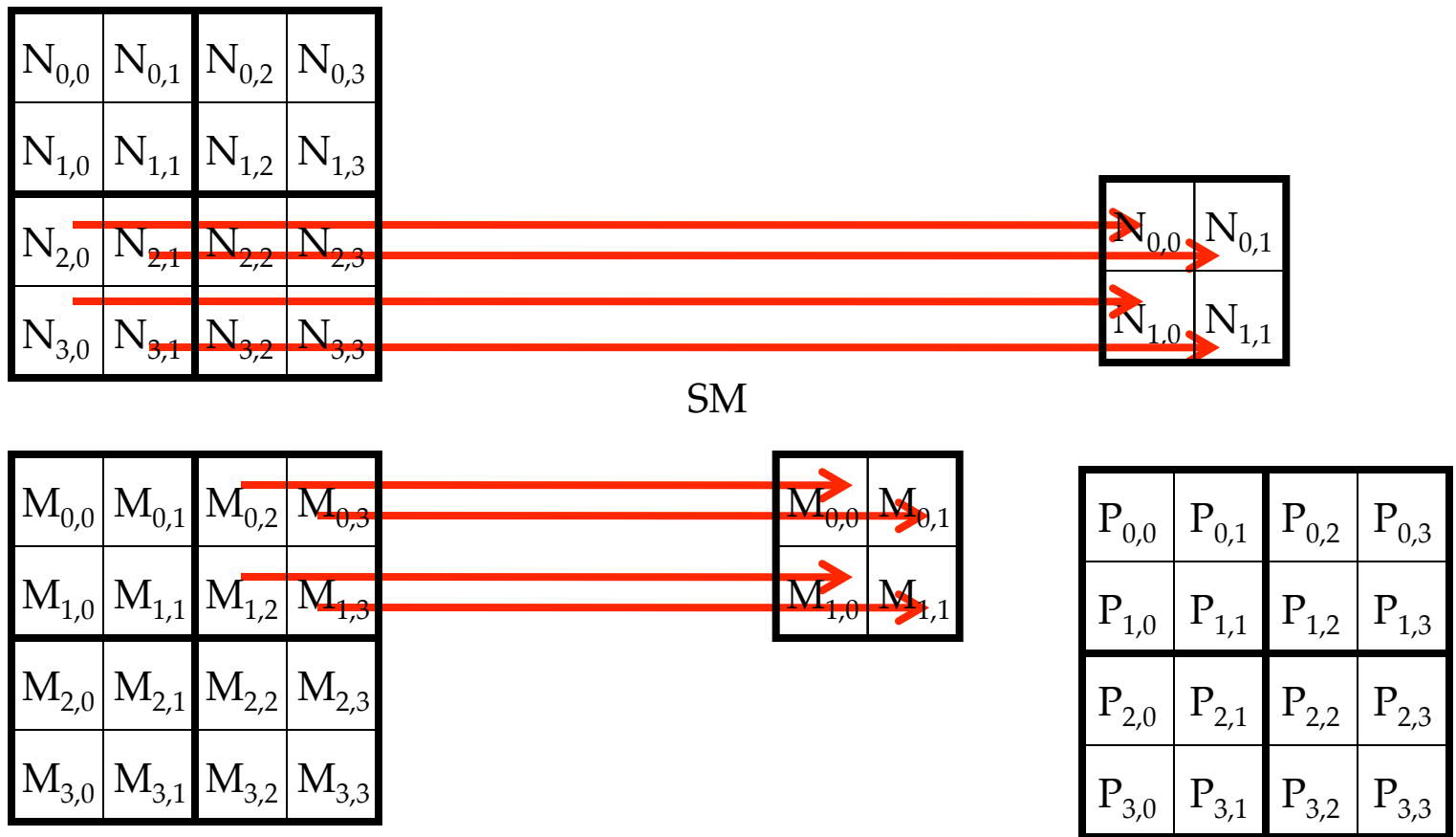
Work for Block (0,0)

$N_{0,0}$	$N_{0,1}$	$N_{0,2}$	$N_{0,3}$
$N_{1,0}$	$N_{1,1}$	$N_{1,2}$	$N_{1,3}$
$N_{2,0}$	$N_{2,1}$	$N_{2,2}$	$N_{2,3}$
$N_{3,0}$	$N_{3,1}$	$N_{3,2}$	$N_{3,3}$

$M_{0,0}$	$M_{0,1}$	$M_{0,2}$	$M_{0,3}$
$M_{1,0}$	$M_{1,1}$	$M_{1,2}$	$M_{1,3}$
$M_{2,0}$	$M_{2,1}$	$M_{2,2}$	$M_{2,3}$
$M_{3,0}$	$M_{3,1}$	$M_{3,2}$	$M_{3,3}$



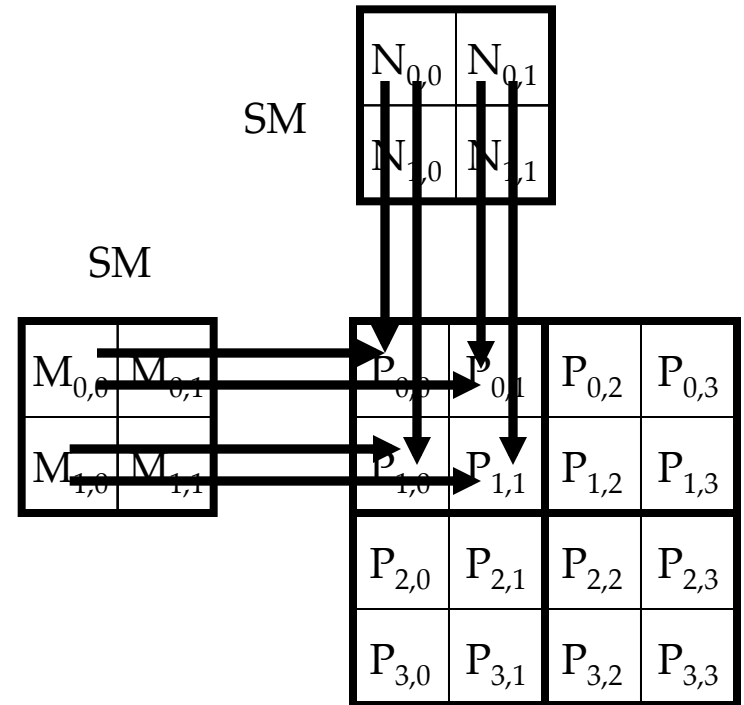
Work for Block (0,0)



Work for Block (0,0)

$N_{0,0}$	$N_{0,1}$	$N_{0,2}$	$N_{0,3}$
$N_{1,0}$	$N_{1,1}$	$N_{1,2}$	$N_{1,3}$
$N_{2,0}$	$N_{2,1}$	$N_{2,2}$	$N_{2,3}$
$N_{3,0}$	$N_{3,1}$	$N_{3,2}$	$N_{3,3}$

$M_{0,0}$	$M_{0,1}$	$M_{0,2}$	$M_{0,3}$
$M_{1,0}$	$M_{1,1}$	$M_{1,2}$	$M_{1,3}$
$M_{2,0}$	$M_{2,1}$	$M_{2,2}$	$M_{2,3}$
$M_{3,0}$	$M_{3,1}$	$M_{3,2}$	$M_{3,3}$



Barrier Synchronization

- An API function call in CUDA
 - `__syncthreads()`
- All threads in the same block must reach the `__syncthreads()` before any can move on
- Best used to coordinate tiled algorithms
 - To ensure that all elements of a tile are loaded
 - To ensure that all elements of a tile are consumed

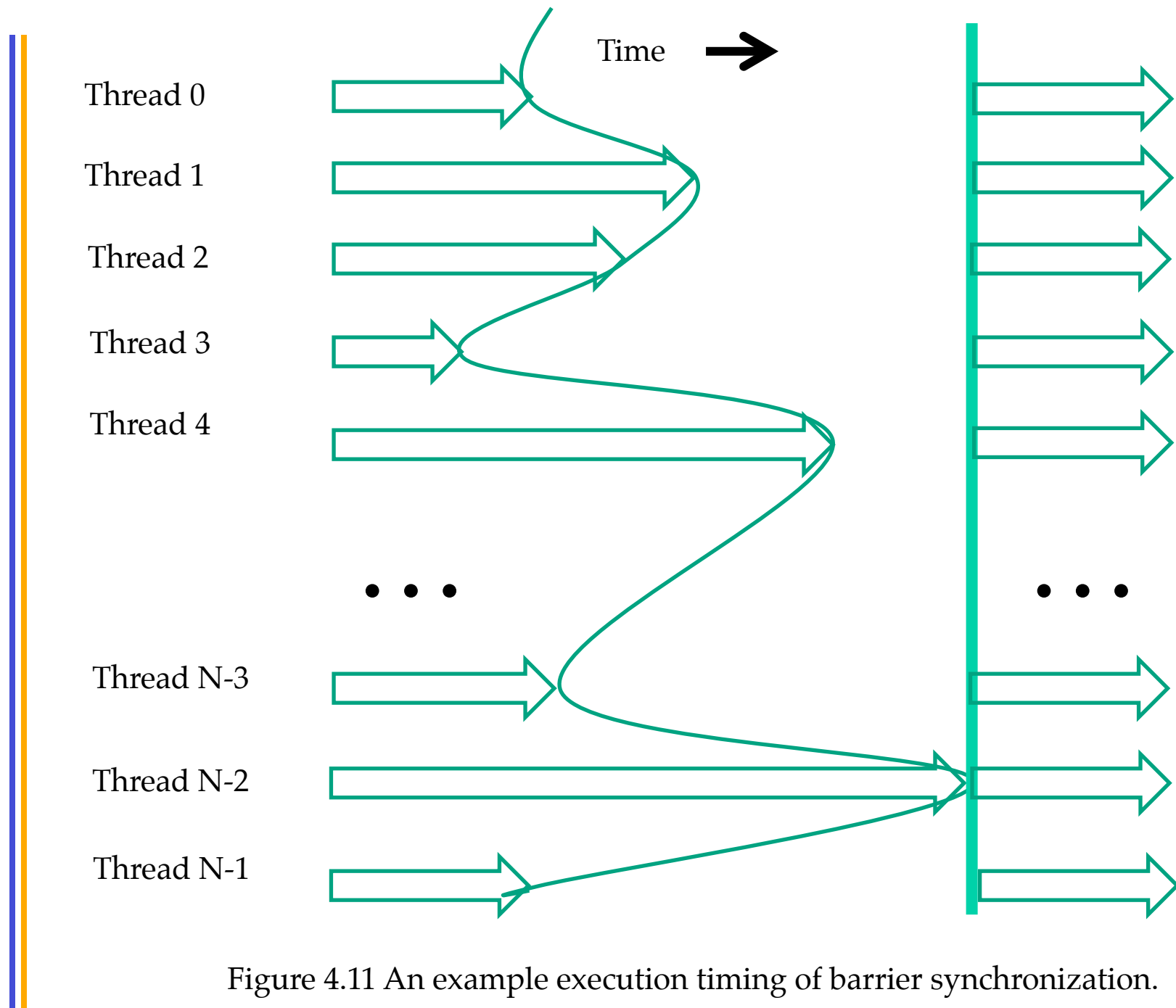


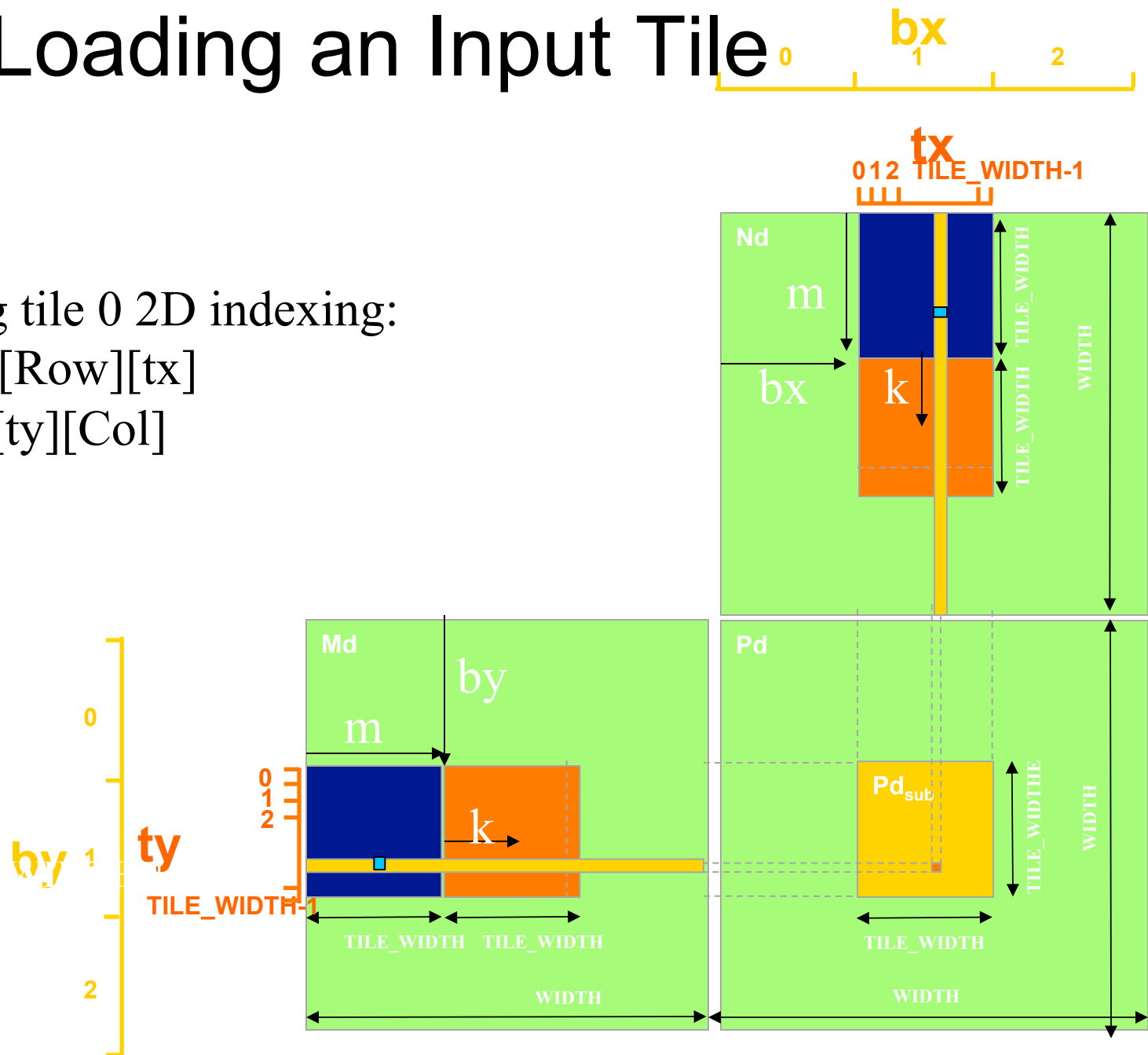
Figure 4.11 An example execution timing of barrier synchronization.

Loading an Input Tile

Accessing tile 0 2D indexing:

$M[\text{Row}][\text{tx}]$

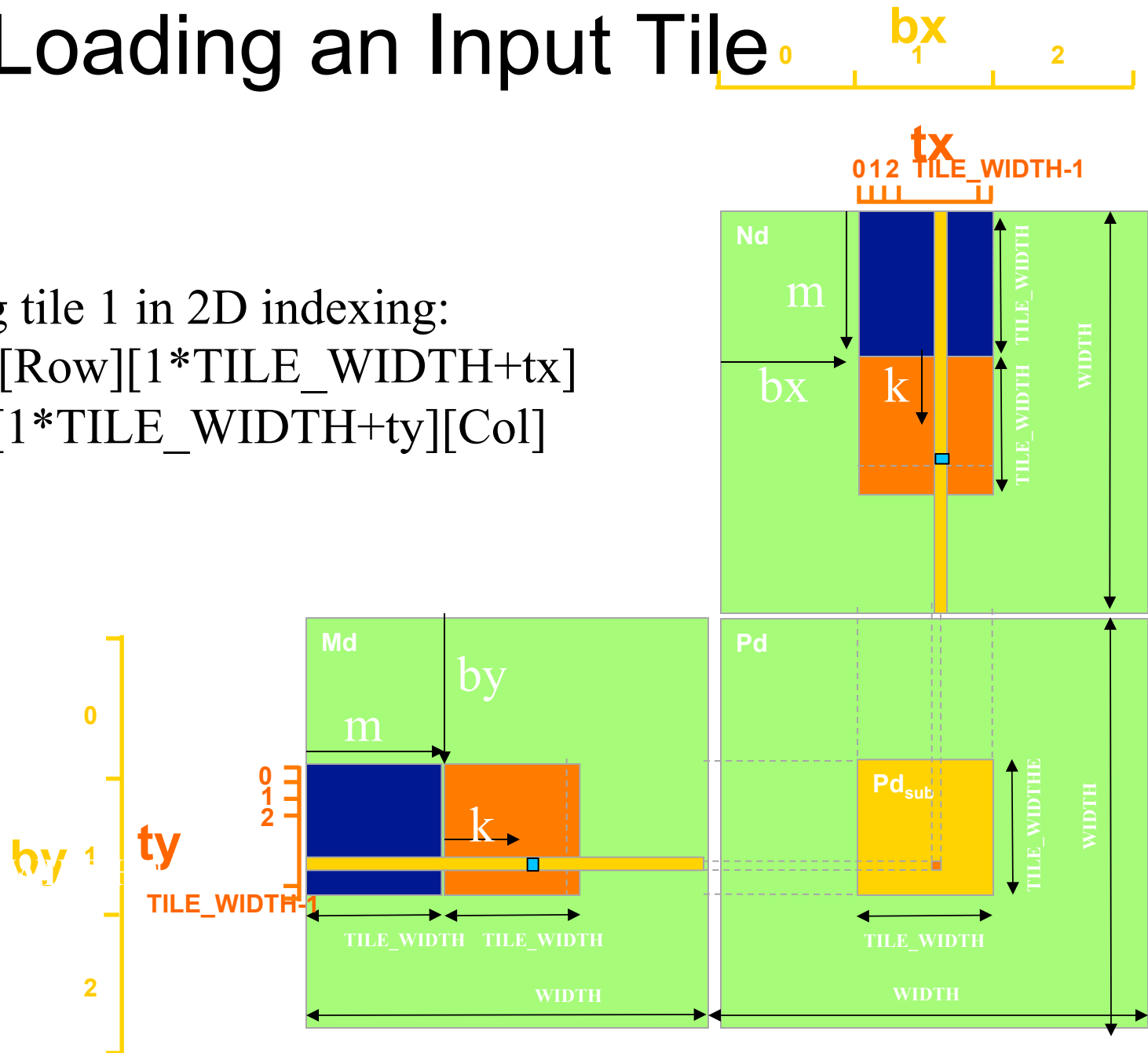
$N[\text{ty}][\text{Col}]$



Loading an Input Tile

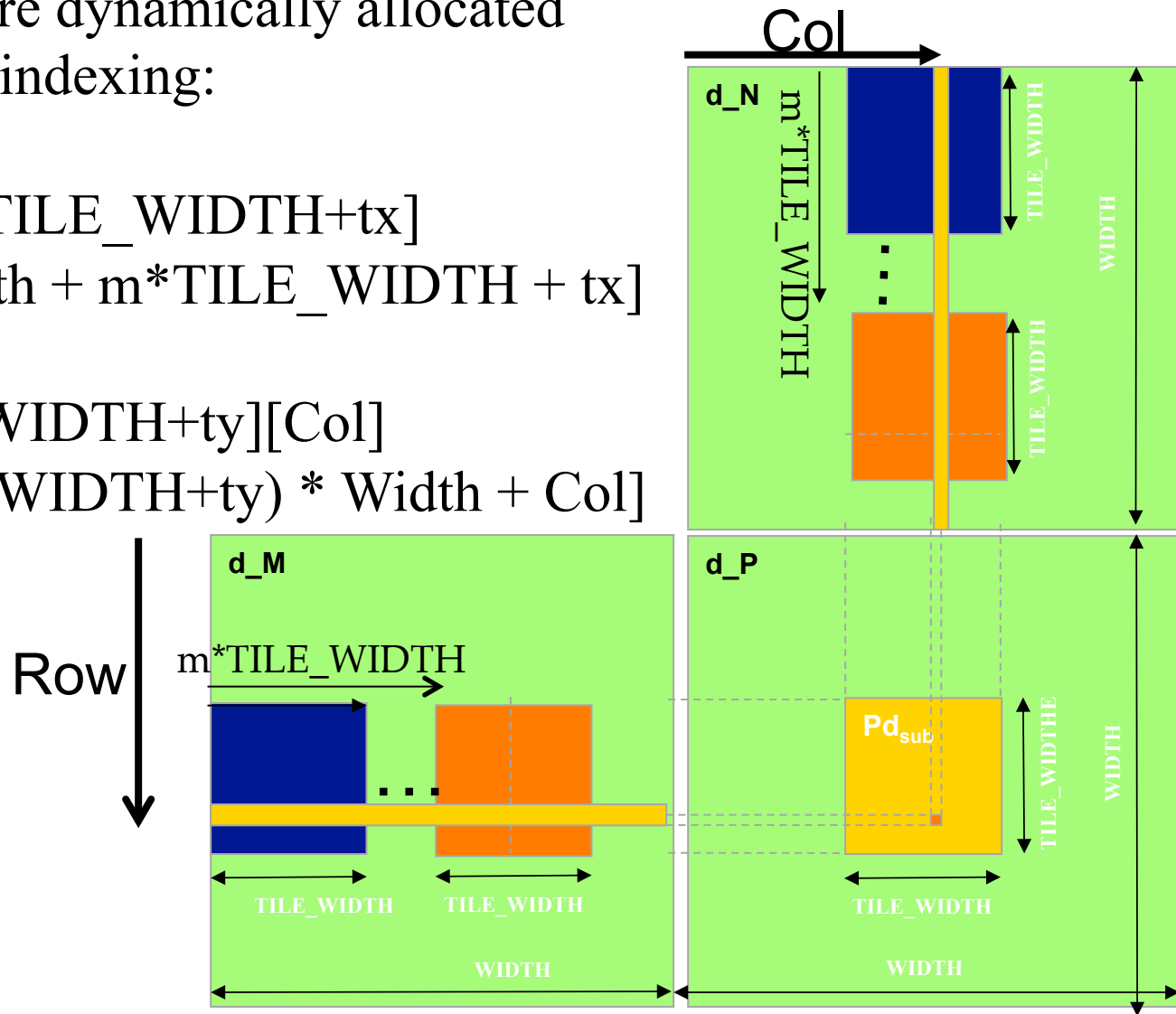
Accessing tile 1 in 2D indexing:

$$M[\text{Row}][1 * \text{TILE_WIDTH} + \text{tx}]$$

$$N[1 * \text{TILE_WIDTH} + \text{ty}][\text{Col}]$$


Loading Input Tile m

However, M and N are dynamically allocated and can only use 1D indexing:

$$M[\text{Row}][m * \text{TILE_WIDTH} + tx]$$
$$M[\text{Row} * \text{Width} + m * \text{TILE_WIDTH} + tx]$$
$$N[m * \text{TILE_WIDTH} + ty][\text{Col}]$$
$$N[(m * \text{TILE_WIDTH} + ty) * \text{Width} + \text{Col}]$$


Tiled Matrix Multiplication Kernel

```
__global__ void MatrixMulKernel(float* d_M, float* d_N, float* d_P, int Width)
{
1.  __shared__ float ds_M[TILE_WIDTH][TILE_WIDTH];
2.  __shared__ float ds_N[TILE_WIDTH][TILE_WIDTH];

3.  int bx = blockIdx.x;  int by = blockIdx.y;
4.  int tx = threadIdx.x; int ty = threadIdx.y;

// Identify the row and column of the Pd element to work on
5.  int Row = by * TILE_WIDTH + ty;
6.  int Col = bx * TILE_WIDTH + tx;
7.  float Pvalue = 0;
// Loop over the Md and Nd tiles required to compute the Pd element
8.  for (int m = 0; m < Width/TILE_WIDTH; ++m) {
// Collaborative loading of Md and Nd tiles into shared memory
9.      ds_M[ty][tx] = d_M[Row*Width + m*TILE_WIDTH+tx];
10.     ds_N[ty][tx] = d_N[Col+(m*TILE_WIDTH+ty)*Width];
11.     __syncthreads();
12.     for (int k = 0; k < TILE_WIDTH; ++k)
13.         Pvalue += ds_M[ty][k] * ds_N[k][tx];
14.     __syncthreads();
15. }
16.  d_P[Row*Width+Col] = Pvalue;
}
```

Compare with the Base Kernel

```
__global__ void MatrixMulKernel(float* d_M, float* d_N, float* d_P, int Width)
{
    // Calculate the row index of the Pd element and M
    int Row = blockIdx.y*TILE_WIDTH + threadIdx.y;
    // Calculate the column index of Pd and N
    int Col = blockIdx.x*TILE_WIDTH + threadIdx.x;

    float Pvalue = 0;
    // each thread computes one element of the block sub-matrix
    for (int k = 0; k < Width; ++k)
        Pvalue += d_M[Row*Width+k] * d_N[k*Width+Col];

    d_P[Row*Width+Col] = Pvalue;
}
```

First-order Size Considerations

- Each **thread block** should have many threads
 - TILE_WIDTH of 16 gives $16 \times 16 = 256$ threads
 - TILE_WIDTH of 32 gives $32 \times 32 = 1024$ threads
- For 16, each block performs $2 \times 256 = 512$ float loads from global memory for $256 * (2 \times 16) = 8,192$ mul/add operations.
- For 32, each block performs $2 \times 1024 = 2048$ float loads from global memory for $1024 * (2 \times 32) = 65,536$ mul/add operations

Shared Memory and Threading

- Each SM in Fermi has 16KB or 48KB shared memory*
 - SM size is implementation dependent!
 - For `TILE_WIDTH` = 16, each thread block uses $2 \times 256 \times 4B = 2KB$ of shared memory.
 - Can potentially have up to 8 Thread Blocks actively executing
 - This allows up to $8 \times 512 = 4,096$ pending loads. (2 per thread, 256 threads per block)
 - The next `TILE_WIDTH` 32 would lead to $2 \times 32 \times 32 \times 4B = 8KB$ shared memory usage per thread block, allowing 2 or 6 thread blocks active at the same time
- Using 16x16 tiling, we reduce the accesses to the global memory by a factor of 16
 - The 150GB/s bandwidth can now support $(150/4) \times 16 = 600GFLOPS!$

*Configurable vs L1, total 64KB

Boundary conditions

- What to do if the matrix size is not a multiple of width?
 - Tricky problem, lets work through an example
- Too many boundary checks can cause control divergence and overhead
- Something that you have to work through for lab 2
 - I'll start a piazza discussion on the topic

Device Query

- Number of devices in the system

```
int dev_count;  
cudaGetDeviceCount( &dev_count);
```

- Capability of devices

```
cudaDeviceProp      dev_prop;  
for (i = 0; i < dev_count; i++) {  
    cudaGetDeviceProperties( &dev_prop, i);  
  
    // decide if device has sufficient resources and capabilities  
}
```

- `cudaDeviceProp` is a built-in C structure type
 - `dev_prop.dev_prop.maxThreadsPerBlock`
 - `dev_prop.sharedMemoryPerBlock`
 - ...

Summary- Typical Structure of a CUDA Program

- Global variables declaration
 - `__host__`
 - `__device__... __global__, __constant__, __texture__`
 - Function prototypes
 - `__global__ void kernelOne(...)`
 - `float handyFunction(...)`
 - Main ()
 - allocate memory space on the device – `cudaMalloc(&d_GlbIVarPtr, bytes )`
 - transfer data from host to device – `cudaMemcpy(d_GlbIVarPtr, h_Gl...)`
 - execution configuration setup
 - kernel call – `kernelOne<<<execution configuration>>>( args... );`
 - transfer results from device to host – `cudaMemcpy(h_GlbIVarPtr,...)`
 - optional: compare against golden (host computed) solution
 - Kernel – `void kernelOne(type args,...)`
 - variables declaration - `auto, __shared__`
 - automatic variables transparently assigned to registers
 - `syncthreads()...`
 - Other functions
 - `float handyFunction(int inVar...);`
- 
- repeat
as
needed



**ANY MORE QUESTIONS?
READ CHAPTER 5!**