



# CS/EE 217: GPU Architecture and Parallel Programming

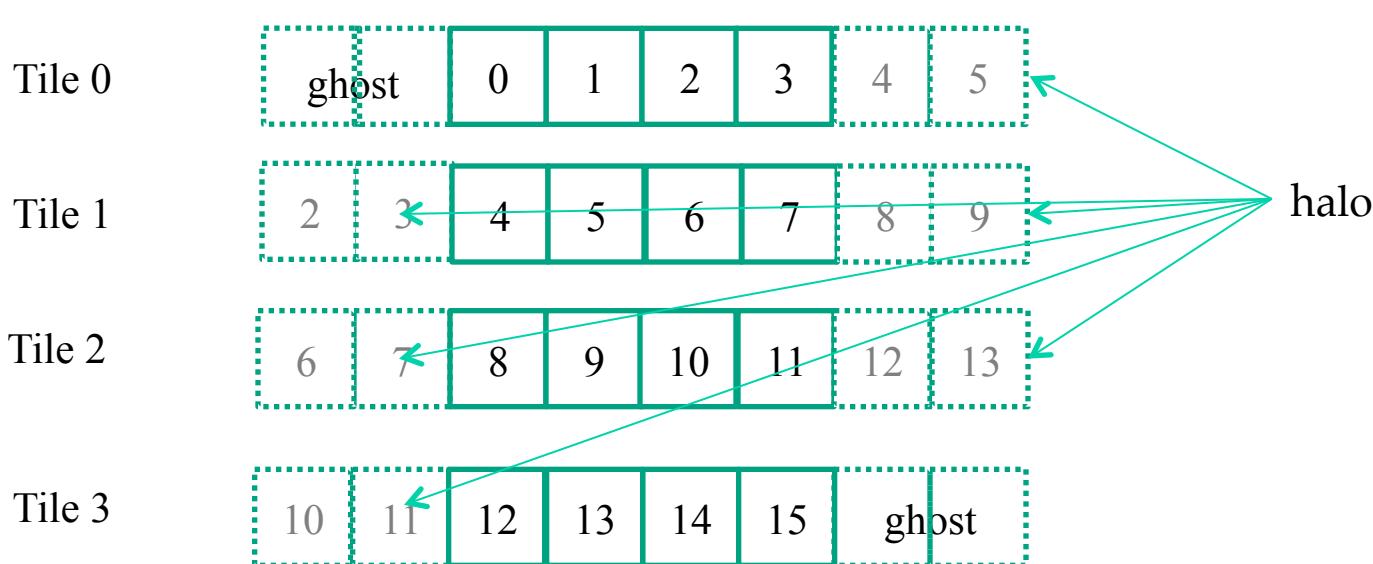
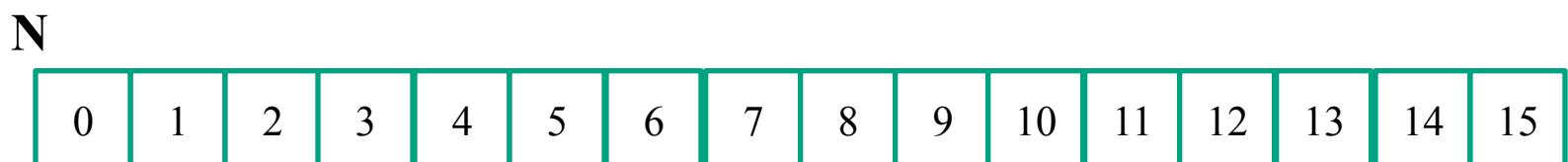
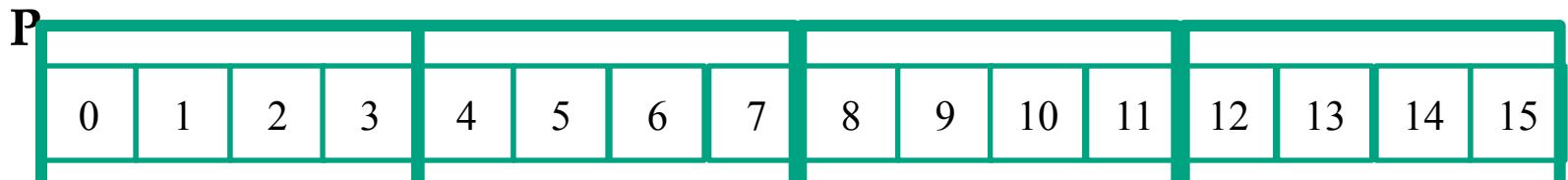
## Tiled Convolution



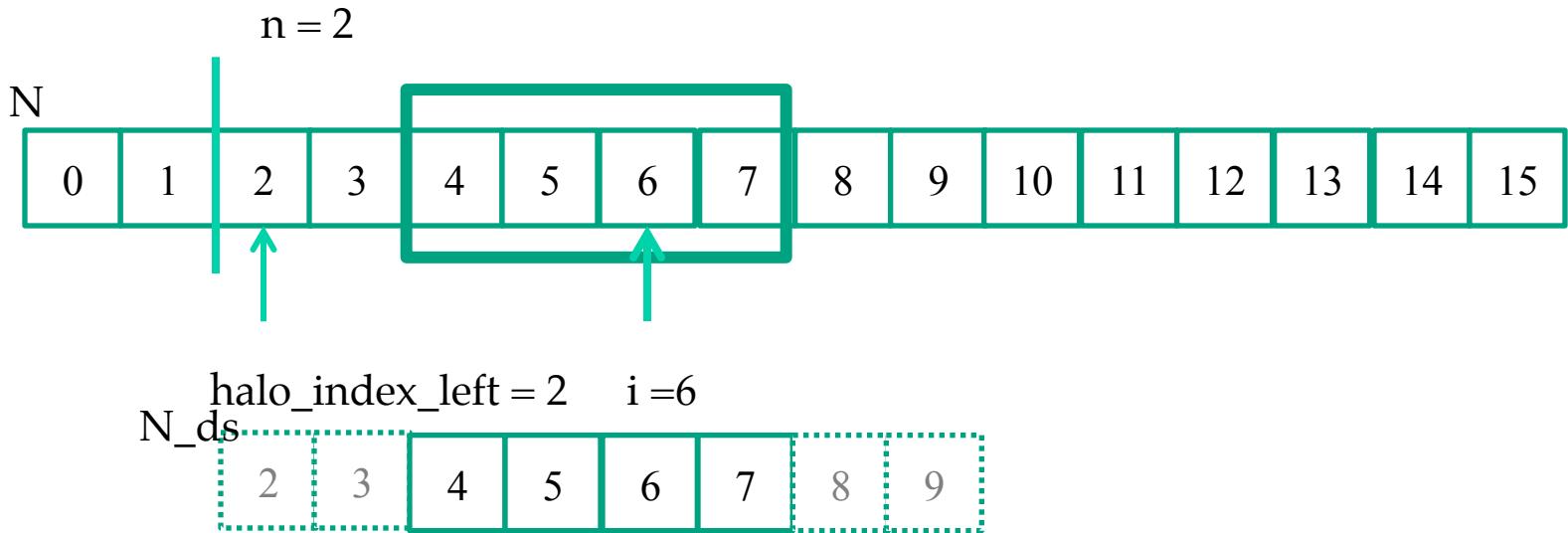
# Objective

- To learn about tiled convolution algorithms
  - Some intricate aspects of tiling algorithms
  - Output tiles versus input tiles

# Tiled 1D Convolution Basic Idea

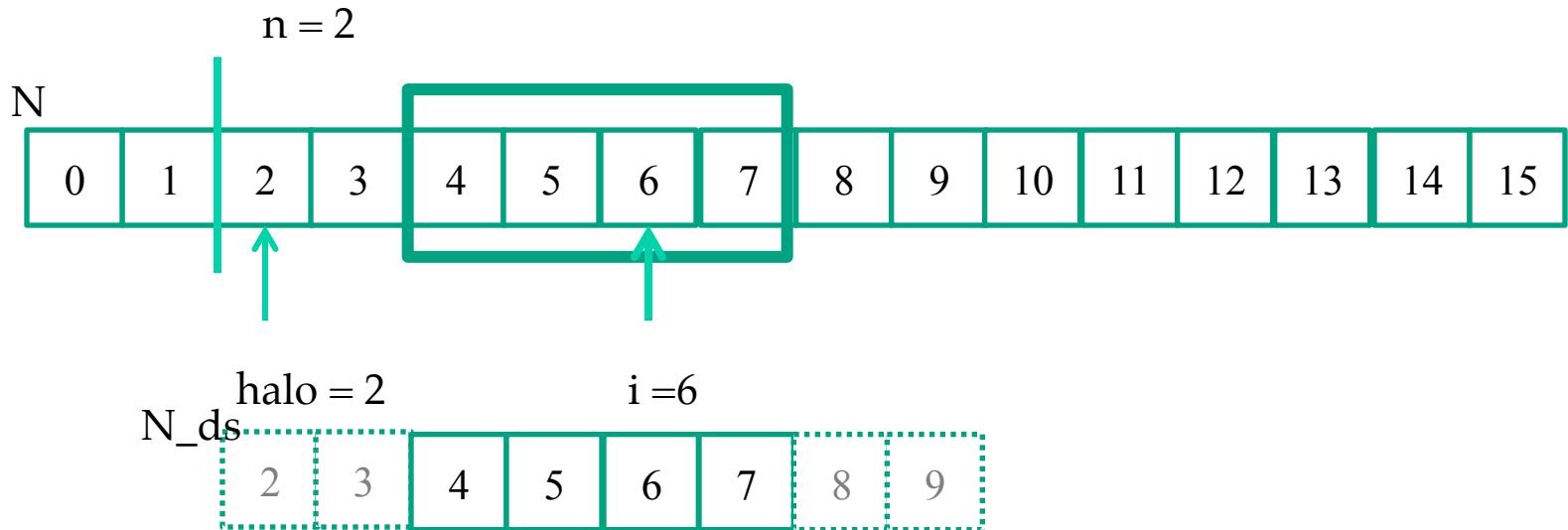


# Loading the left halo



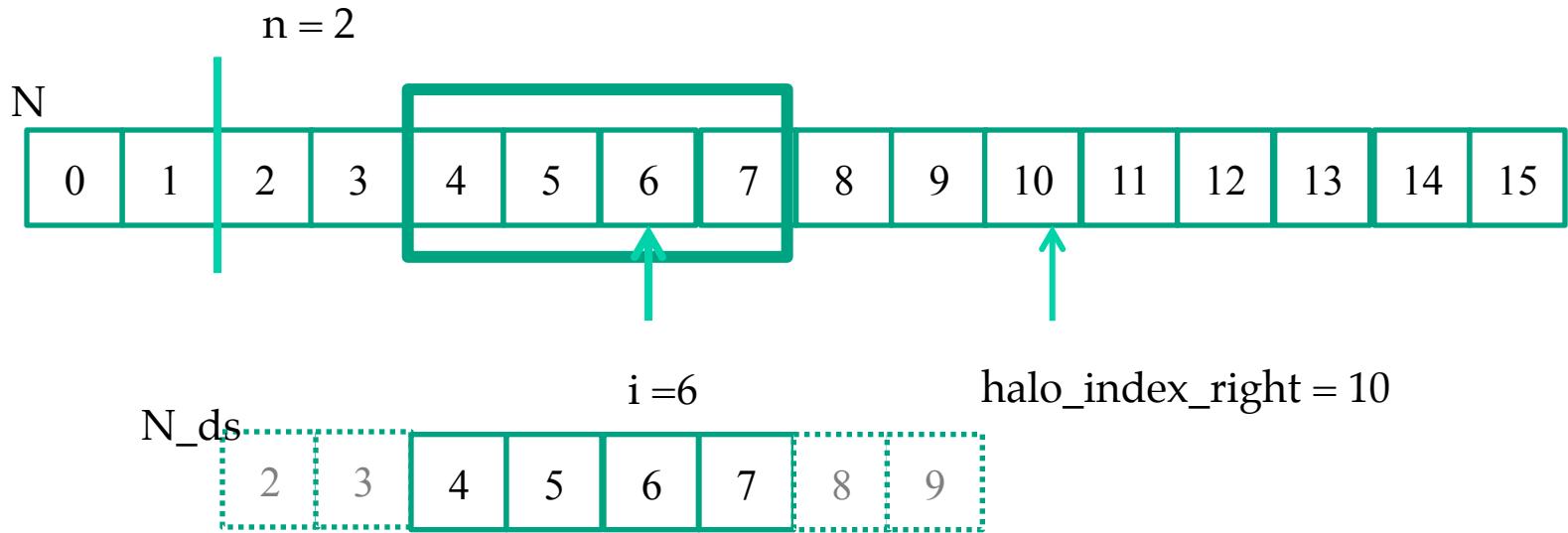
```
int n = Mask_Width/2;
int halo_index_left = (blockIdx.x - 1)*blockDim.x + threadIdx.x;
if (threadIdx.x >= blockDim.x - n) {
    N_ds[threadIdx.x - (blockDim.x - n)] =
        (halo_index_left < 0) ? 0 : N[halo_index_left];
}
```

# Loading the internal elements



```
 $N_{ds}[n + threadIdx.x] = N[blockIdx.x * blockDim.x + threadIdx.x];$ 
```

# Loading the right halo



```
int halo_index_right = (blockIdx.x + 1)*blockDim.x + threadIdx.x;
if (threadIdx.x < n) {
    N_ds[n + blockDim.x + threadIdx.x] =
        (halo_index_right >= Width) ? 0 : N[halo_index_right];
}
```

```
__global__ void convolution_1D_basic_kernel(float *N, float *P, int
Mask_Width,
    int Width) {

    int i = blockIdx.x*blockDim.x + threadIdx.x;
    __shared__ float N_ds[TILE_SIZE + MAX_MASK_WIDTH - 1];

    int n = Mask_Width/2;

    int halo_index_left = (blockIdx.x - 1)*blockDim.x + threadIdx.x;
    if (threadIdx.x >= blockDim.x - n) {
        N_ds[threadIdx.x - (blockDim.x - n)] =
            (halo_index_left < 0) ? 0 : N[halo_index_left];
    }

    N_ds[n + threadIdx.x] = N[blockIdx.x*blockDim.x + threadIdx.x];

    int halo_index_right = (blockIdx.x + 1)*blockDim.x + threadIdx.x;
    if (threadIdx.x < n) {
        N_ds[n + blockDim.x + threadIdx.x] =
            (halo_index_right >= Width) ? 0 : N[halo_index_right];
    }

    __syncthreads();

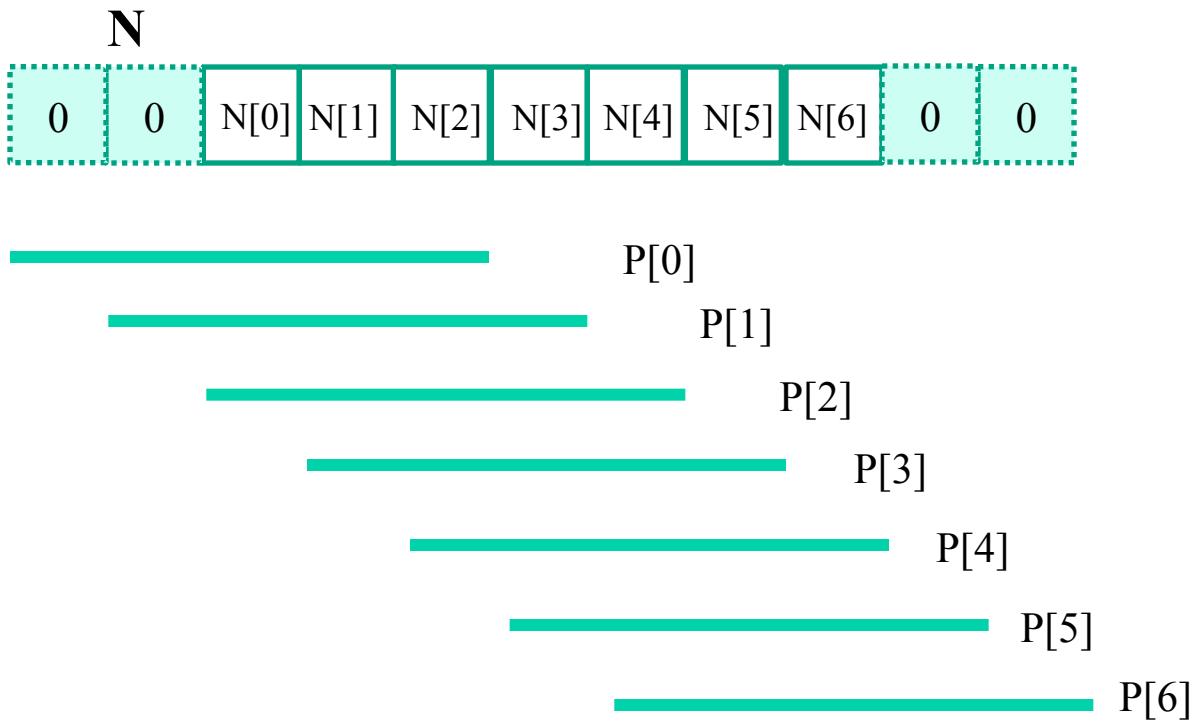
    float Pvalue = 0;
    for(int j = 0; j < Mask_Width; j++) {
        Pvalue += N_ds[threadIdx.x + j]*M[j];
    }
    P[i] = Pvalue;
```

# Shared Memory Data Reuse



- Element 2 is used by thread 4 (1X)
- Element 3 is used by threads 4, 5 (2X)
- Element 4 is used by threads 4, 5, 6 (3X)
- Element 5 is used by threads 4, 5, 6, 7 (4X)
- Element 6 is used by threads 4, 5, 6, 7 (4X)
- Element 7 is used by threads 5, 6, 7 (3X)
- Element 8 is used by threads 6, 7 (2X)
- Element 9 is used by thread 7 (1X)

# Ghost Cells



```

__global__ void convolution_1D_basic_kernel(float *N, float *P, int
Mask_Width,
    int Width) {

    int i = blockIdx.x*blockDim.x + threadIdx.x;
    __shared__ float N_ds[TILE_SIZE];

    N_ds[threadIdx.x] = N[i];

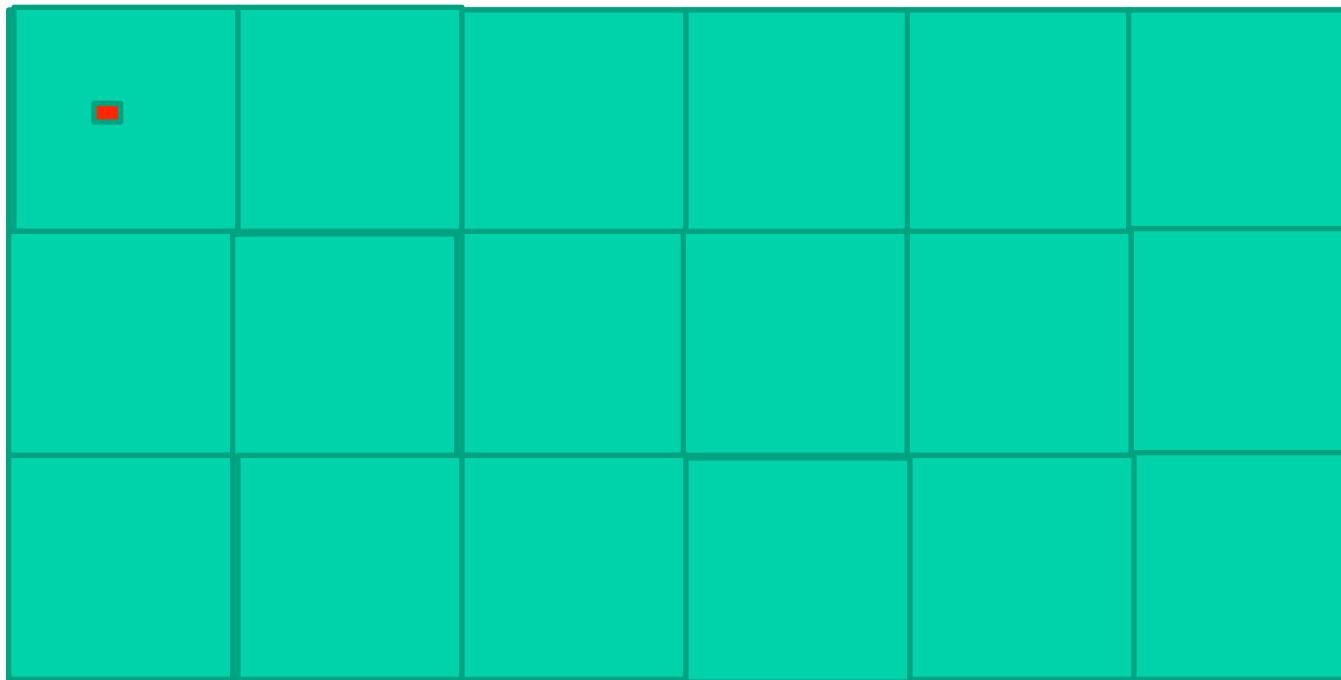
    __syncthreads();

    int This_tile_start_point = blockIdx.x * blockDim.x;
    int Next_tile_start_point = (blockIdx.x + 1) * blockDim.x;
    int N_start_point = i - (Mask_Width/2);
    float Pvalue = 0;
    for (int j = 0; j < Mask_Width; j++) {
        int N_index = N_start_point + j;
        if (N_index >= 0 && N_index < Width) {
            if ((N_index >= This_tile_start_point)
                && (N_index < Next_tile_start_point)) {
                Value += N_ds[threadIdx.x+j-(Mask_Width/2)]*M[j];
            } else {
                Pvalue += N[N_index] * M[j];
            }
        }
    }
    P[i] = Pvalue;
}

```

# 2D convolution with Tiling P

- Use a thread block to calculate a tile of P
  - Thread Block size determined by the TILE\_SIZE



# Tiling N

- Each element in the tile is used in calculating up to MASK\_SIZE \* MASK\_SIZE P elements (all elements in the tile)

3	4	5	6	7
2	3	4	5	6
1	2	3	4	5
2	3	5	6	7
0	1	1	3	1

3	4	5	6	7
2	3	4	5	6
1	2	3	4	5
2	3	5	6	7
0	1	1	3	1

3	4	5	6	7
2	3	4	5	6
1	2	3	4	5
2	3	5	6	7
0	1	1	3	1

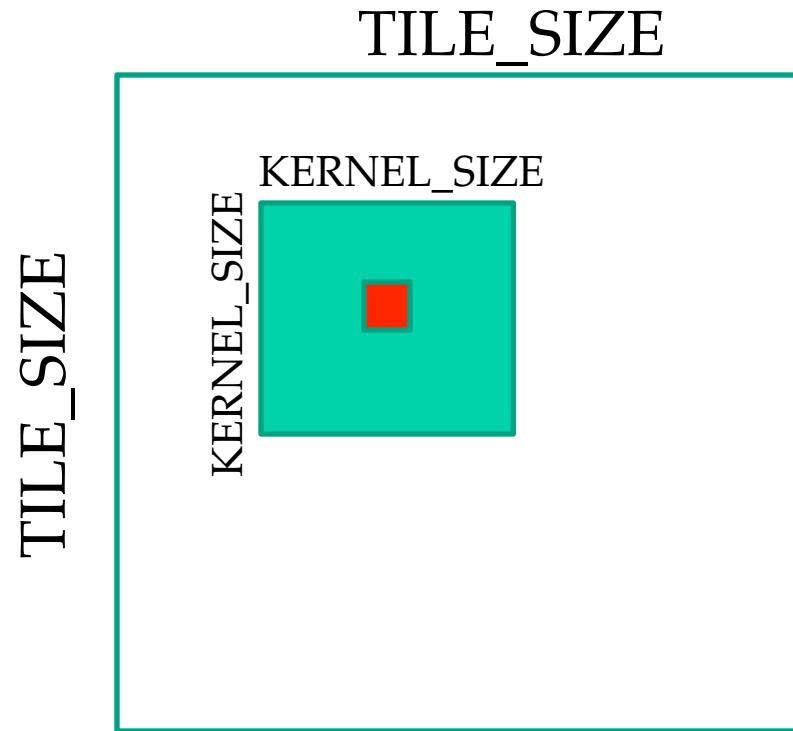
3	4	5	6	7
2	3	4	5	6
1	2	3	4	5
2	3	5	6	7
0	1	1	3	1

3	4	5	6	7
2	3	4	5	6
1	2	3	4	5
2	3	5	6	7
0	1	1	3	1

3	4	5	6	7
2	3	4	5	6
1	2	3	4	5
2	3	5	6	7
0	1	1	3	1

# High-Level Tiling Strategy

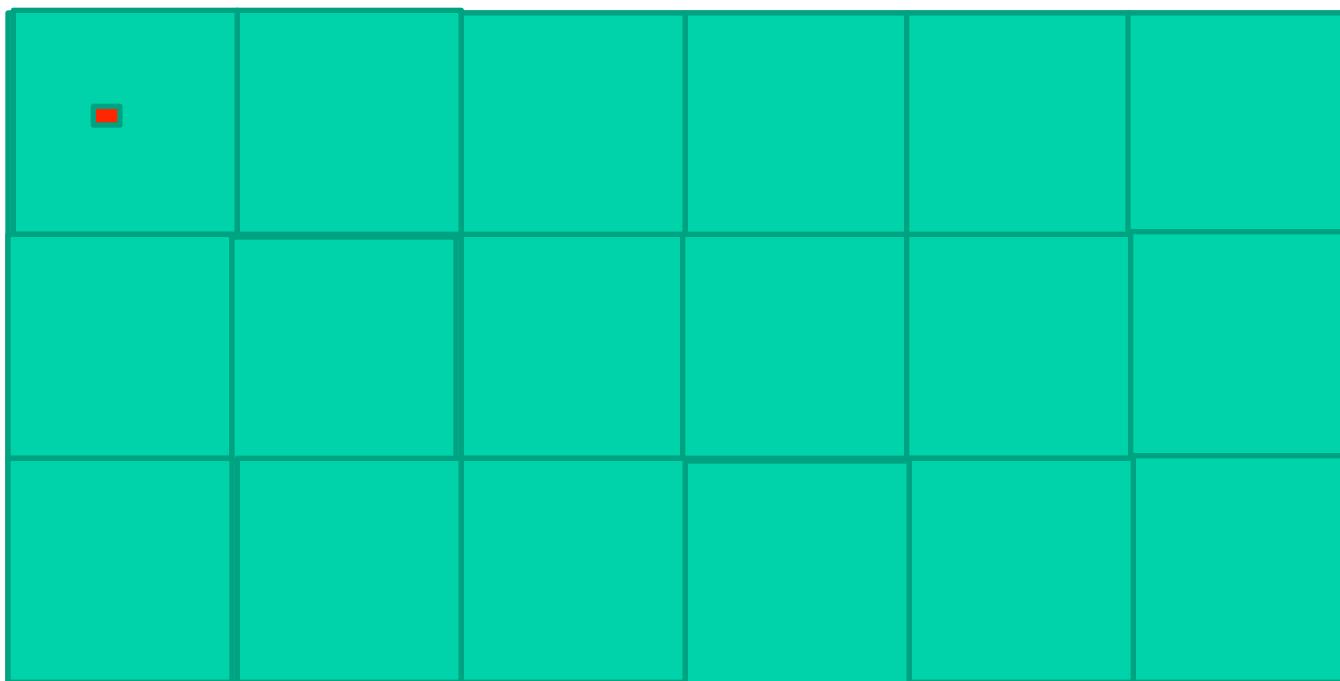
- Load a tile of  $N$  into shared memory (SM)
  - All threads participate in loading
  - A subset of threads then use each  $N$  element in SM



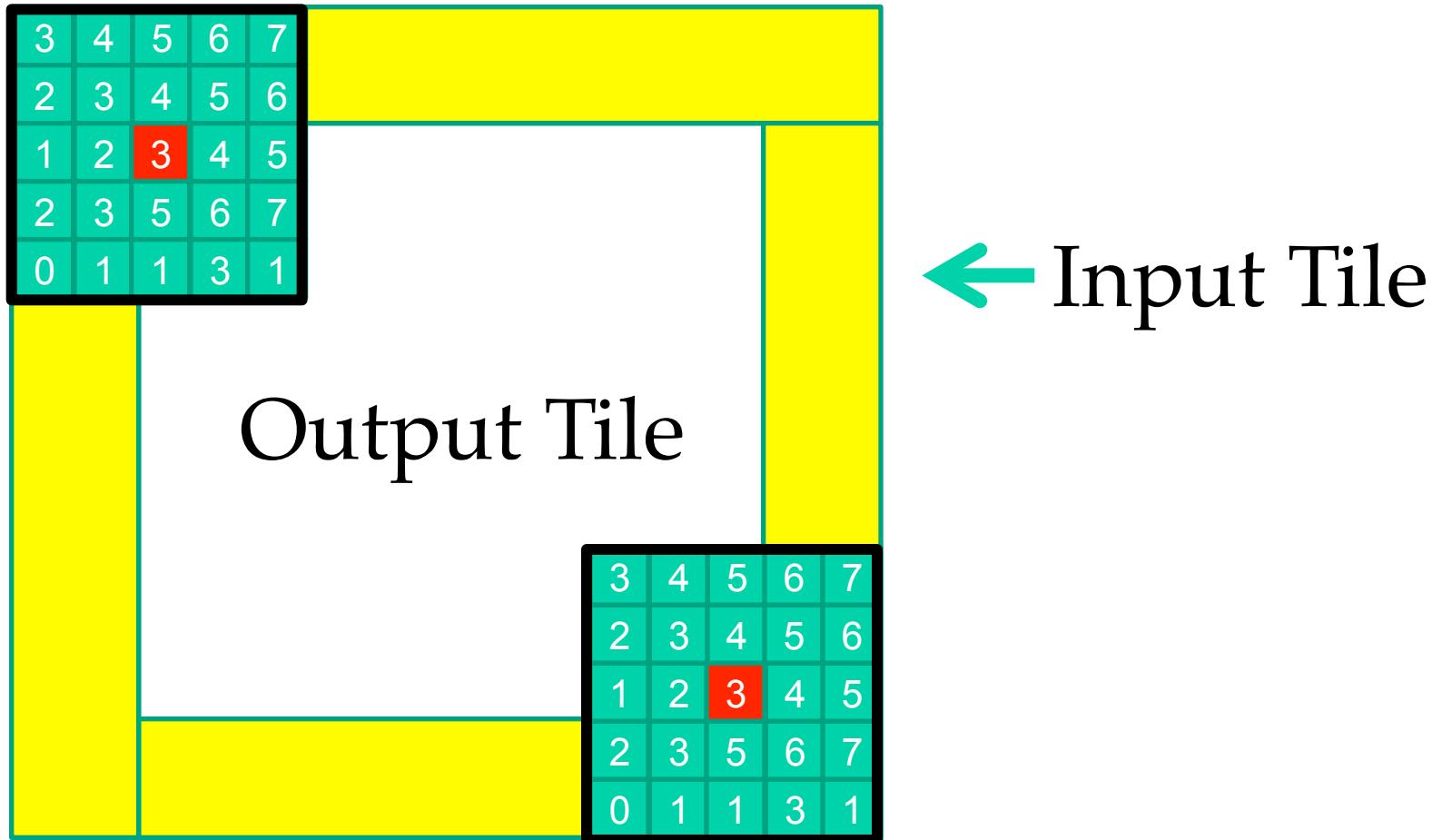
# Output Tiling and Thread Index (P)

- Use a thread block to calculate a tile of P
  - Each output tile is of TILE\_SIZE for both x and y

```
row_o = blockIdx.y * TILE_SIZE + ty;  
col_o = blockIdx.x * TILE_SIZE + tx;
```



# Input tiles need to be larger than output tiles.



# Dealing with Mismatch

- Use a thread block that matches input tile
  - Each thread loads one element of the input tile
  - Some threads do not participate in calculating output
    - There will be if statements and control divergence

# Setting up blocks

```
#define O_TILE_WIDTH 12
#define BLOCK_WIDTH (O_TILE_WIDTH + 4)

dim3 dimBlock (BLOCK_WIDTH, BLOCK_WIDTH);
dim3 dimGrid ((imageWidth - 1)/O_TILE_WIDTH + 1,
(imageHeight-1)/O_TILE_WIDTH+1, 1);
```

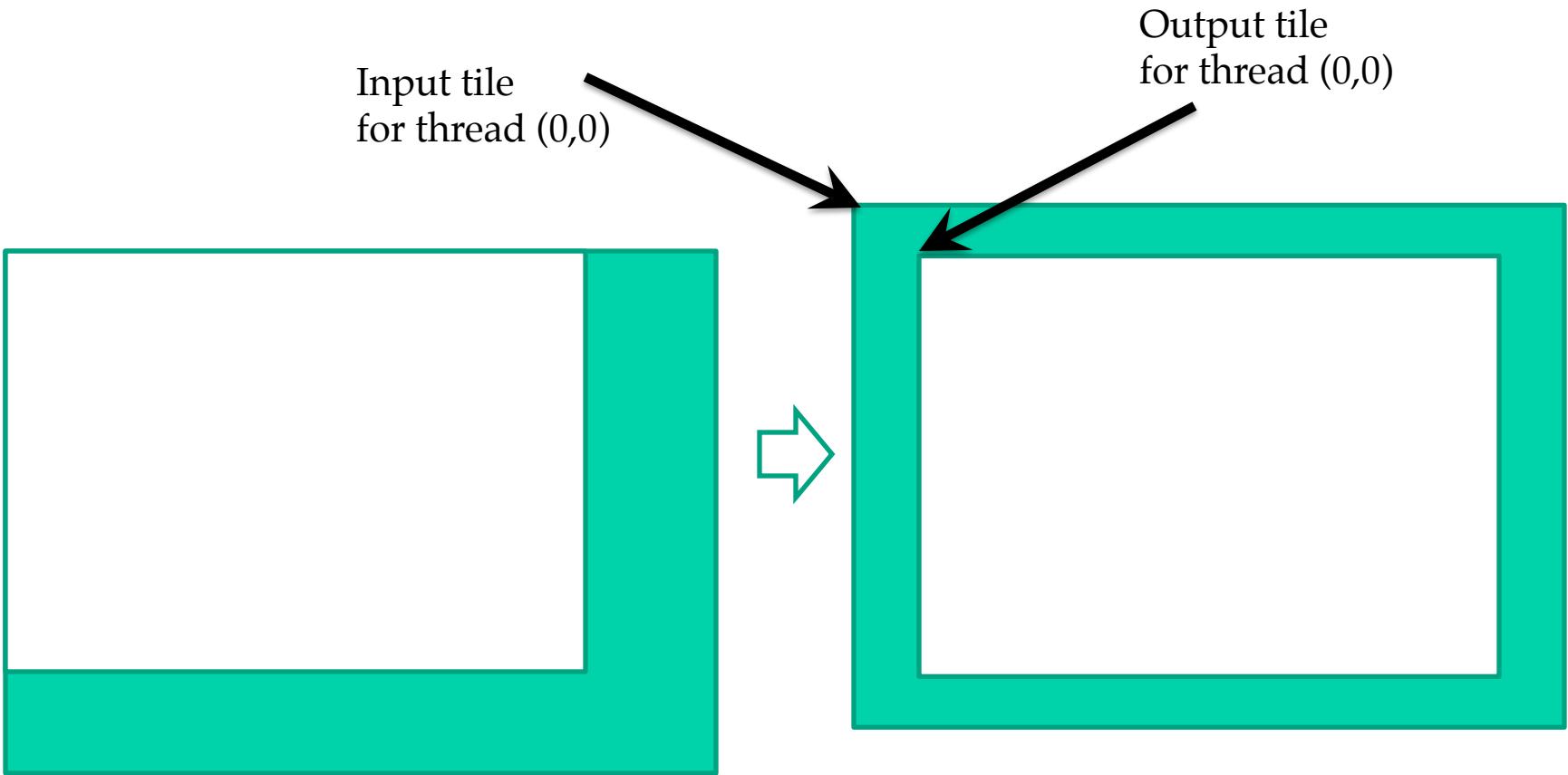
- In general, block width = Tile width + mask width – 1;

# Using constant memory for mask

- Since mask is used by all threads and not modified:
  - All threads in a warp access the same locations at every time
  - Take advantage of the cachable constant memory!
  - Magnify memory bandwidth without consuming shared memory
- Syntax:

```
__global__ void convolution_2D_kernel (float *P,  
                                     *float N, height, width, channels,  
                                     const float __restrict__ *M) {
```

# Shifting from output coordinates to input coordinates

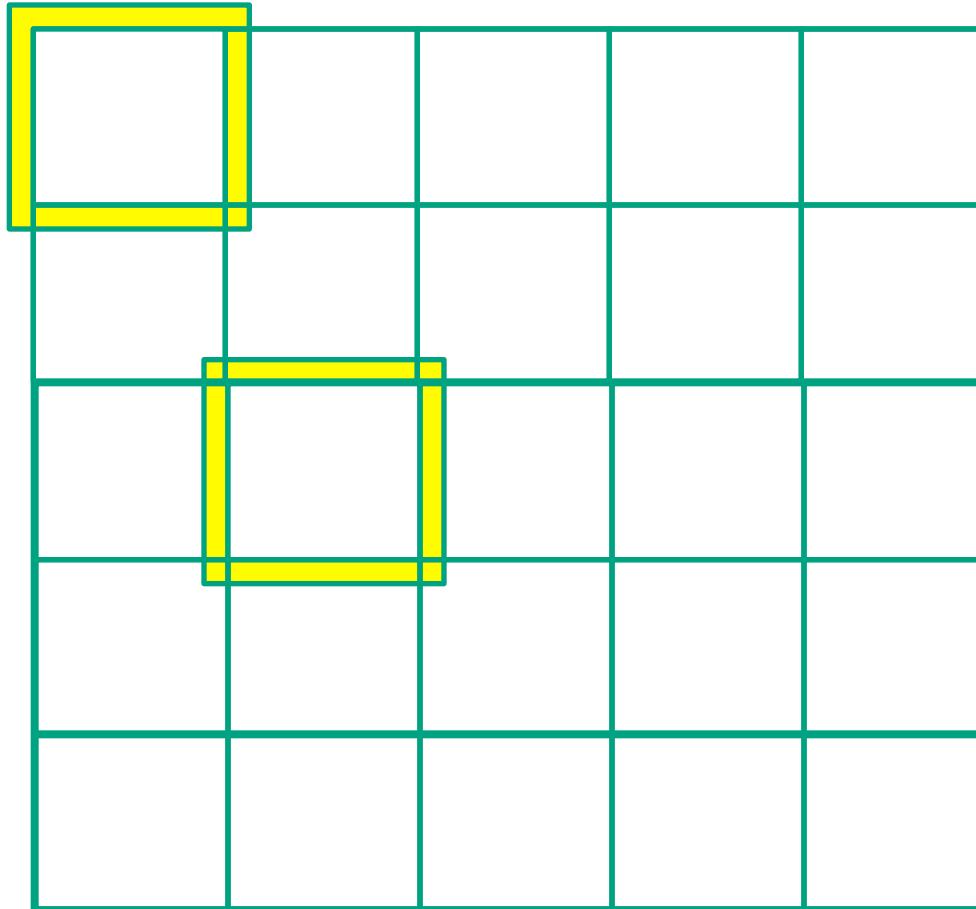


# Shifting from output coordinates to input coordinate

```
int tx = threadIdx.x;  
int ty = threadIdx.y;  
int row_o = blockIdx.y * TILE_SIZE + ty;  
int col_o = blockIdx.x * TILE_SIZE + tx;
```

```
int row_i = row_o - 2; //MASK_SIZE/2  
int col_i = col_o - 2; //MASK_SIZE/2
```

Threads that loads halos outside N  
should return 0.0



# Taking Care of Boundaries

```
float output = 0.0f;  
  
if((row_i >= 0) && (row_i < N.height) &&  
    (col_i >= 0) && (col_i < N.width) ) {  
    Ns[ty][tx] = N.elements[row_i*N.width + col_i];  
}  
else{  
    Ns[ty][tx] = 0.0f;  
}
```

# Some threads do not participate in calculating output.

```
if(ty < TILE_SIZE && tx < TILE_SIZE){  
    for(i = 0; i < MASK_SIZE; i++) {  
        for(j = 0; j < MASK_SIZE; j++) {  
            output += Mc[i][j] * Ns[i+ty][j+tx];  
        }  
    }  
}
```

# Some threads do not write output

```
if(row_o < P.height && col_o < P.width)  
P.elements[row_o * P.width + col_o] = output;
```

# In General

- `BLOCK_SIZE` is limited by the maximum number of threads in a thread block
- Input tile sizes could be could be  $k * \text{TILE\_SIZE} + (\text{MASK\_SIZE}-1)$ 
  - For 1D convolution – what is it for 2D convolution?
  - By having each thread to calculate  $k$  input points (thread coarsening)
  - $k$  is limited by the shared memory size
- `MASK_SIZE` is decided by application needs



**ANY MORE QUESTIONS?  
READ CHAPTER 8**